

Measurements and Characterization of Statistical Variability

Toshiro Hiramoto

Institute of Industrial Science, University of Tokyo

MIRAI-Setele

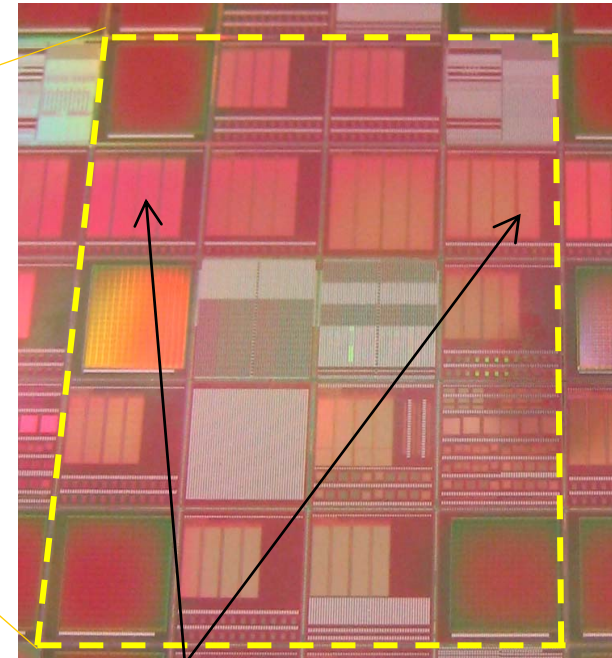
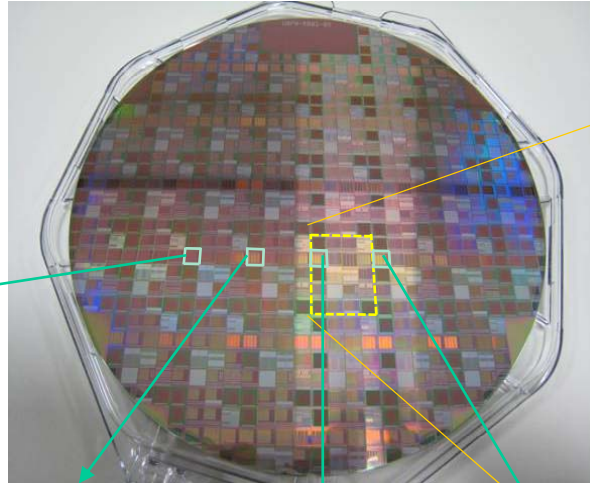
hiramoto@nano.iis.u-tokyo.ac.jp

1. Introduction
2. Variability Measurements and Characterization
 - (1) Drain Current
 - (2) SRAM
3. Summary

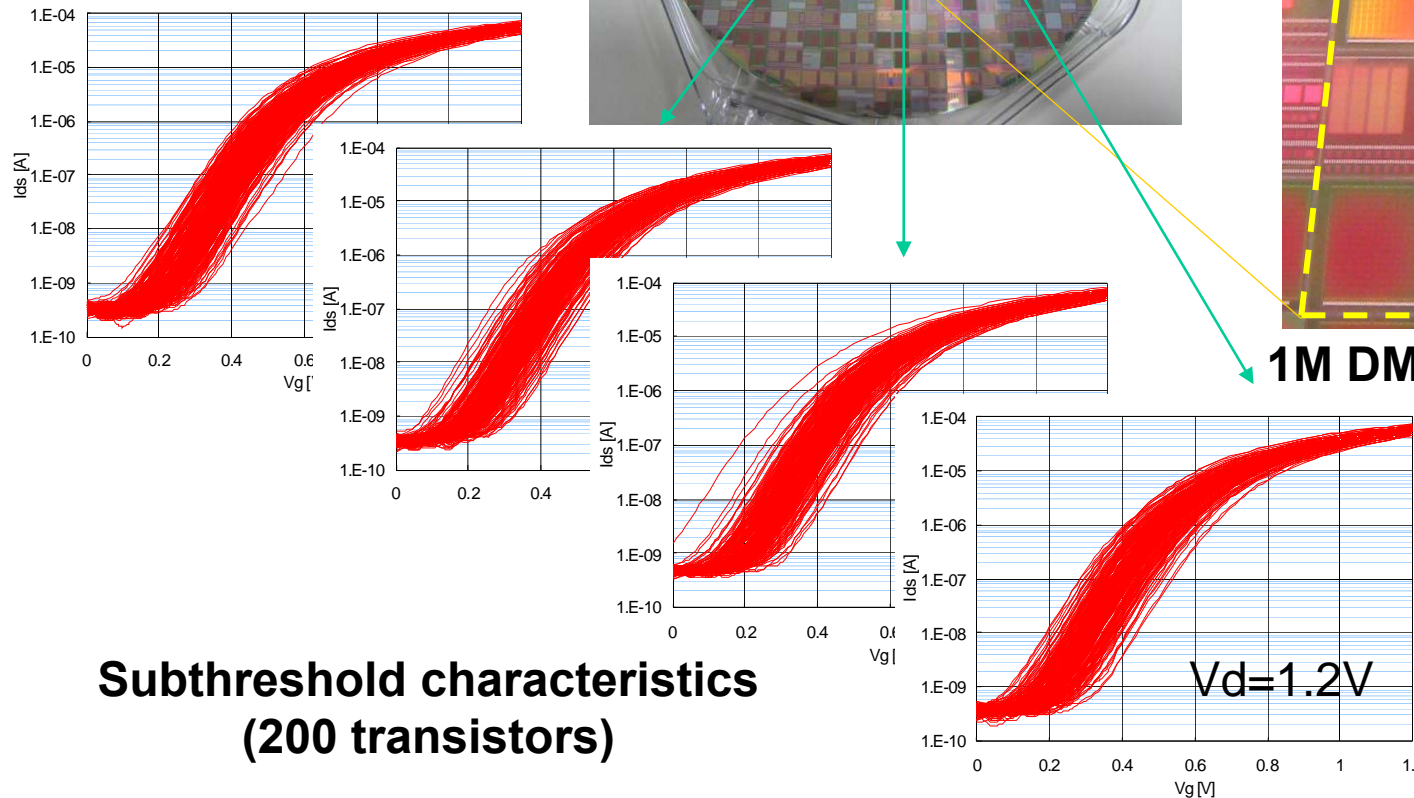
This work is performed in the MIRAI-Project supported by NEDO.

Large-Scale DMA-TEG

1 million transistors
in each chip



1M DMA-TEG



Subthreshold characteristics
(200 transistors)

T. Hiramoto et al., MIRAI
Project Meeting, 2007.

Within Wafer Variation

65nm Technology

L – 60nm

W = 140nm

V_{TH} (V)

■ 0.551-0.555

■ 0.547-0.551

■ 0.543-0.547

■ 0.539-0.543

■ 0.535-0.539

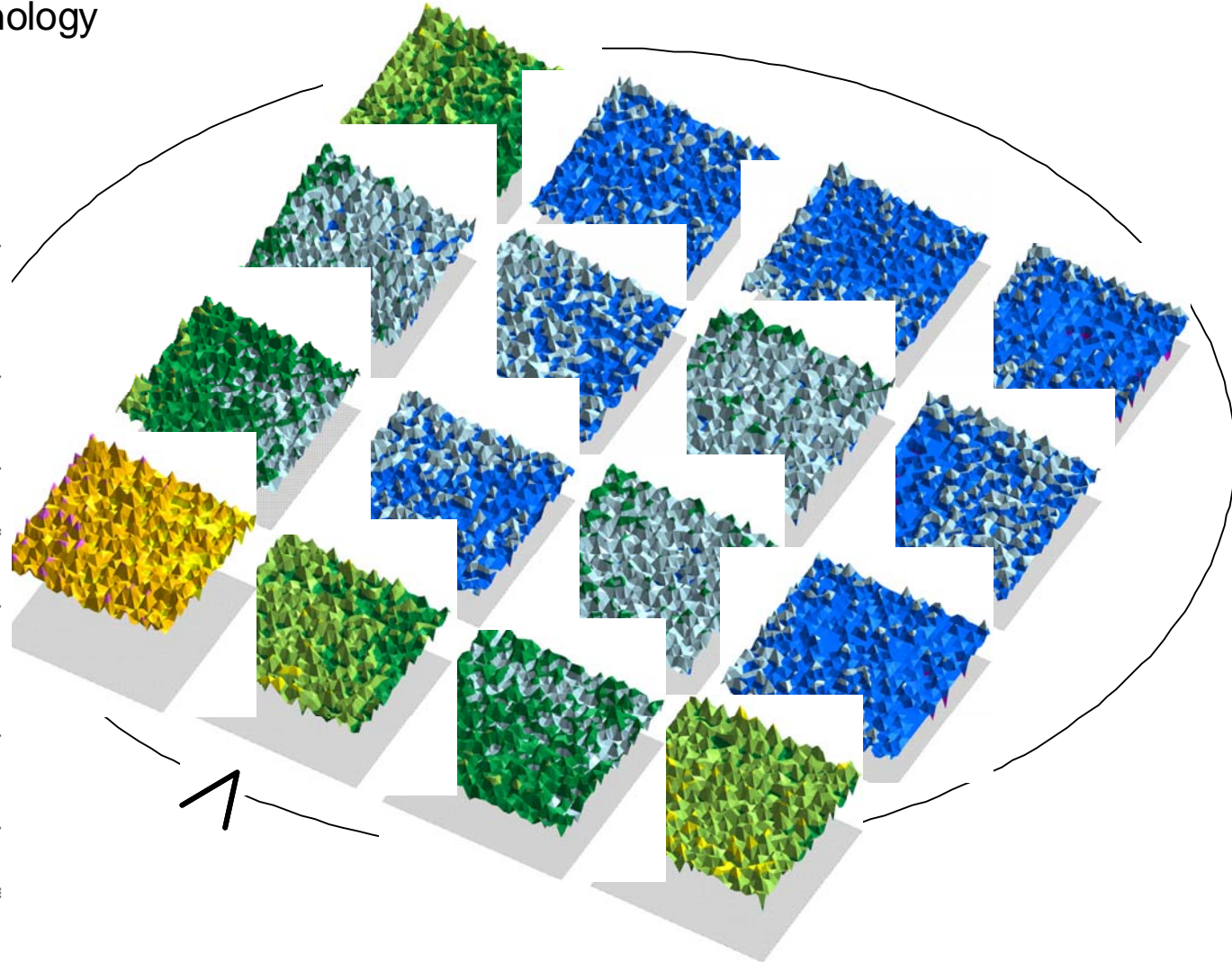
■ 0.531-0.535

■ 0.527-0.531

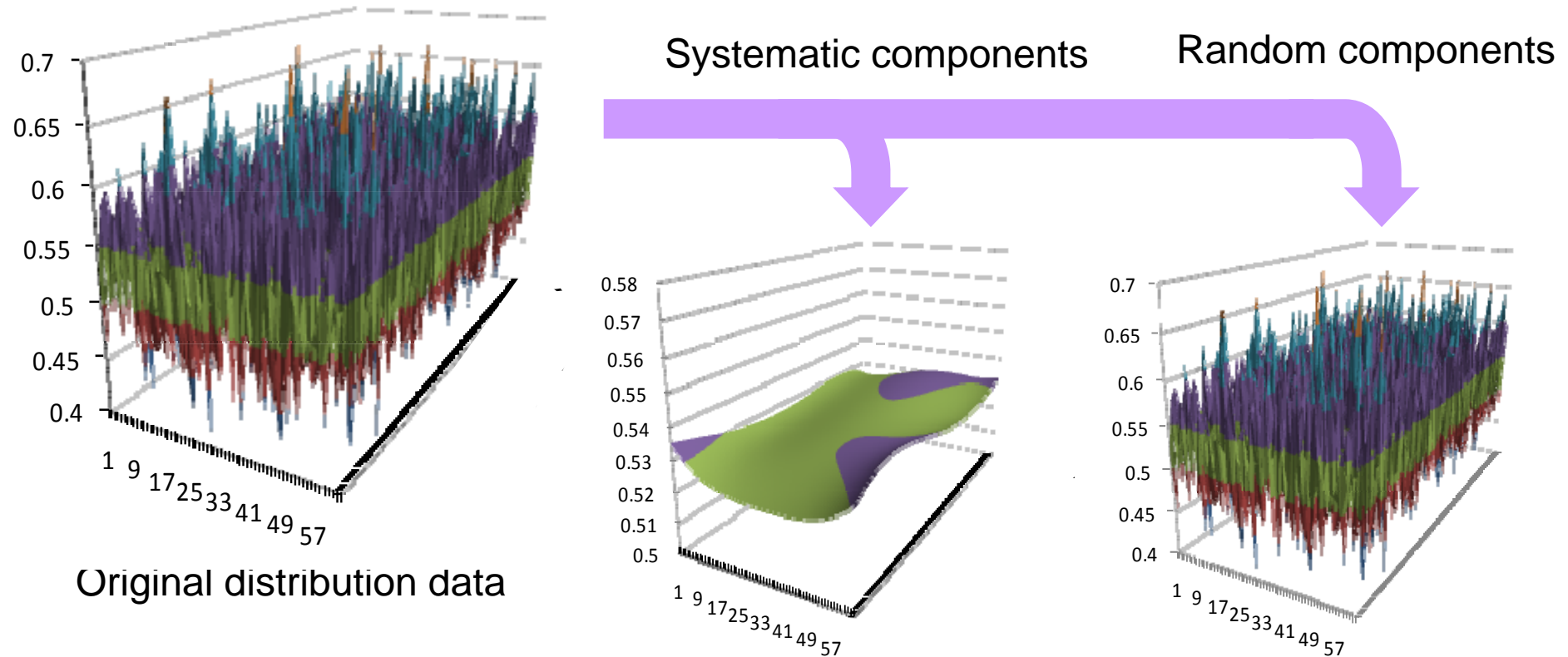
■ 0.523-0.527

■ 0.519-0.523

■ 0.515-0.519



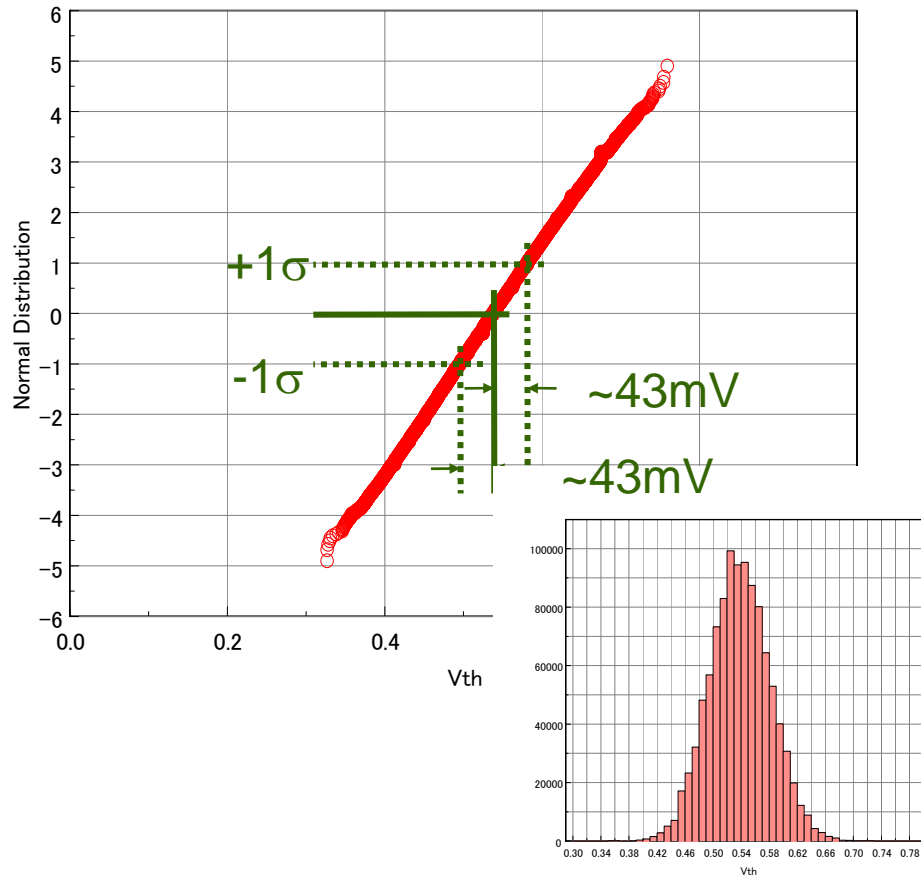
Systematic and Random Components



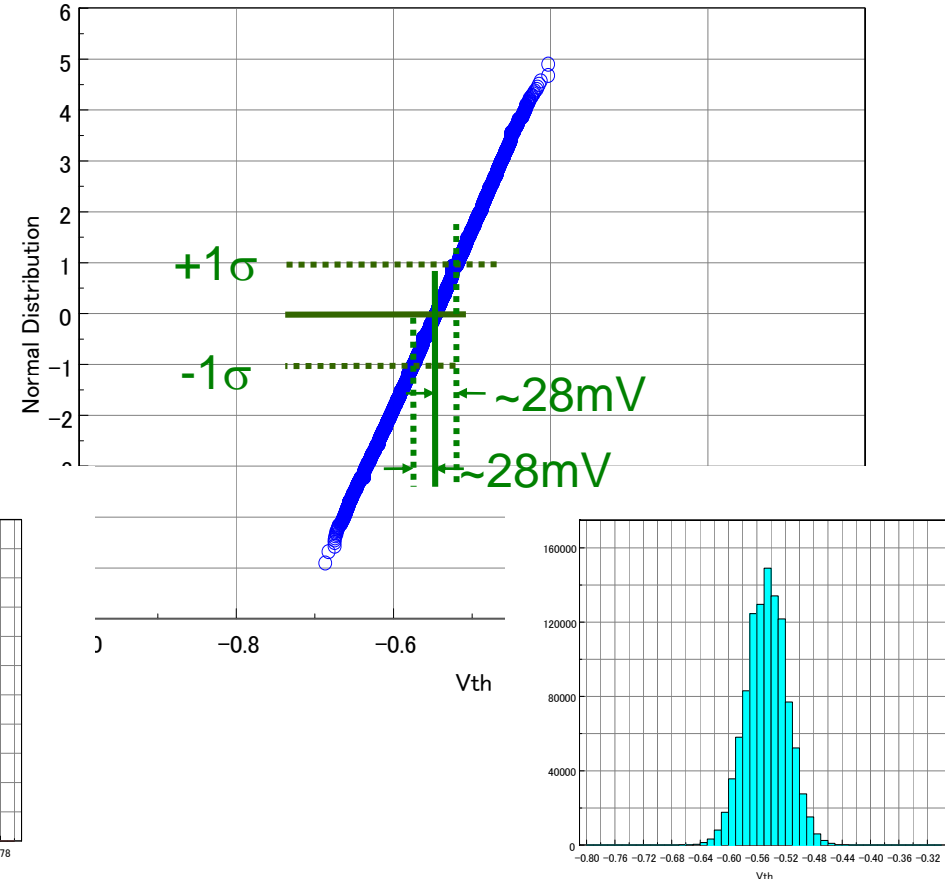
1. Random variation is dominant.
2. Systematic variation is negligible in DMA-TEG.

Vth Distribution of 1 Million Transistors

NFET



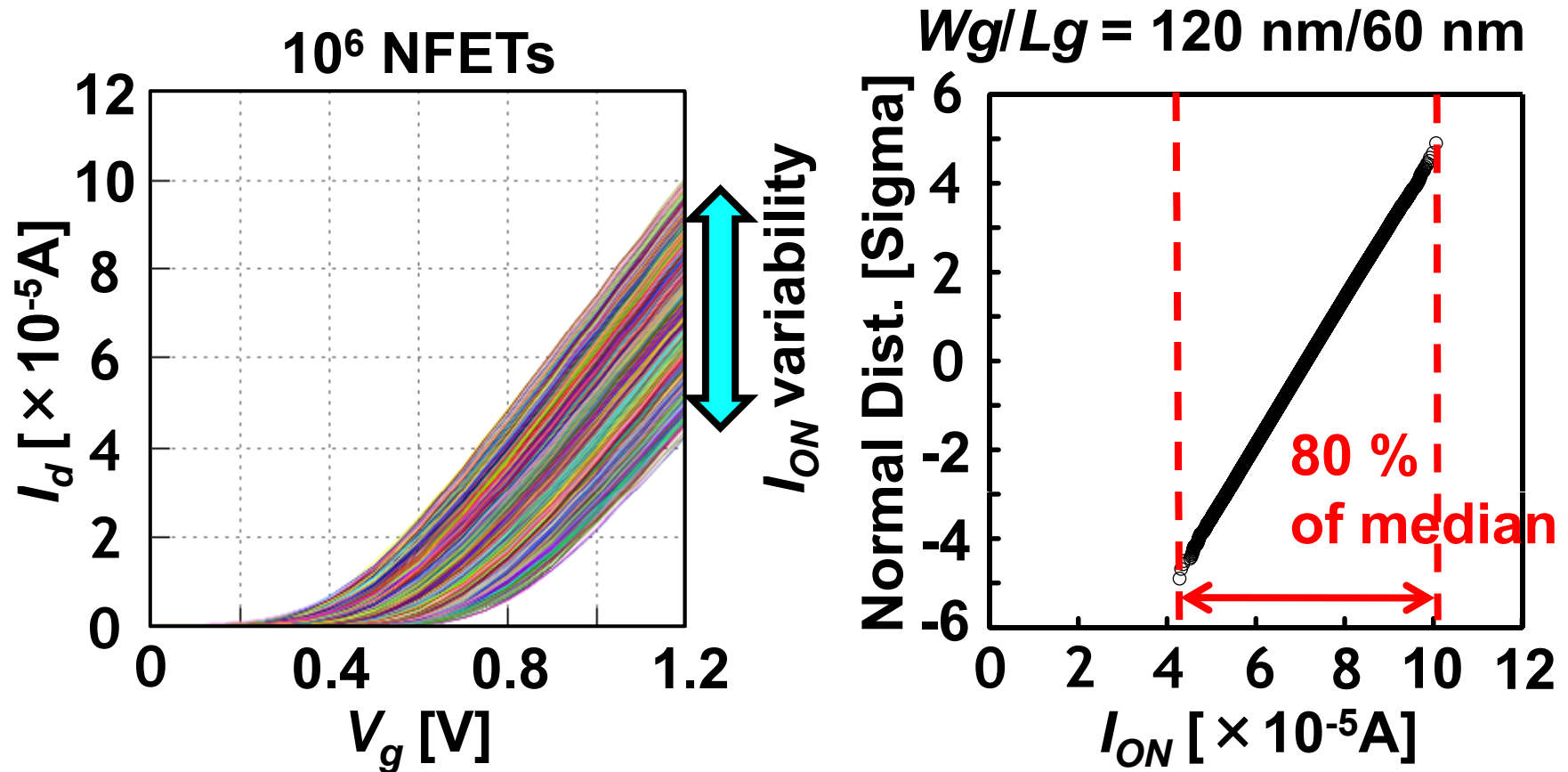
PFET



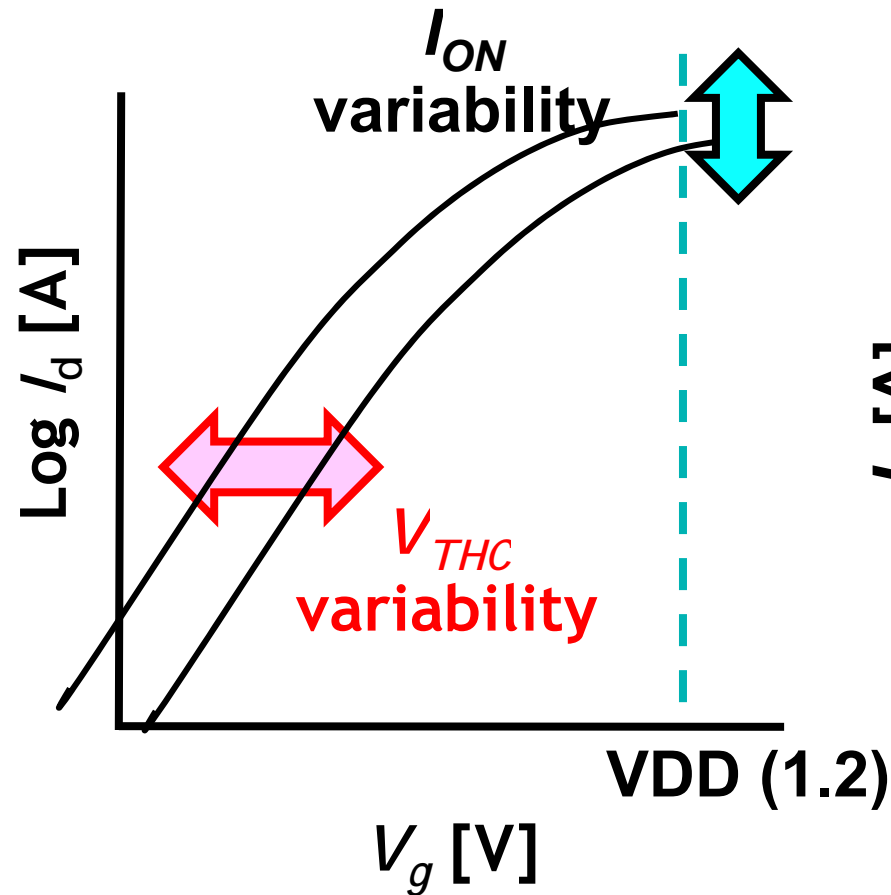
1. Normal distribution up to $\pm 5\sigma$.
2. NFET has larger variations than PFET.

Drain Current Variability

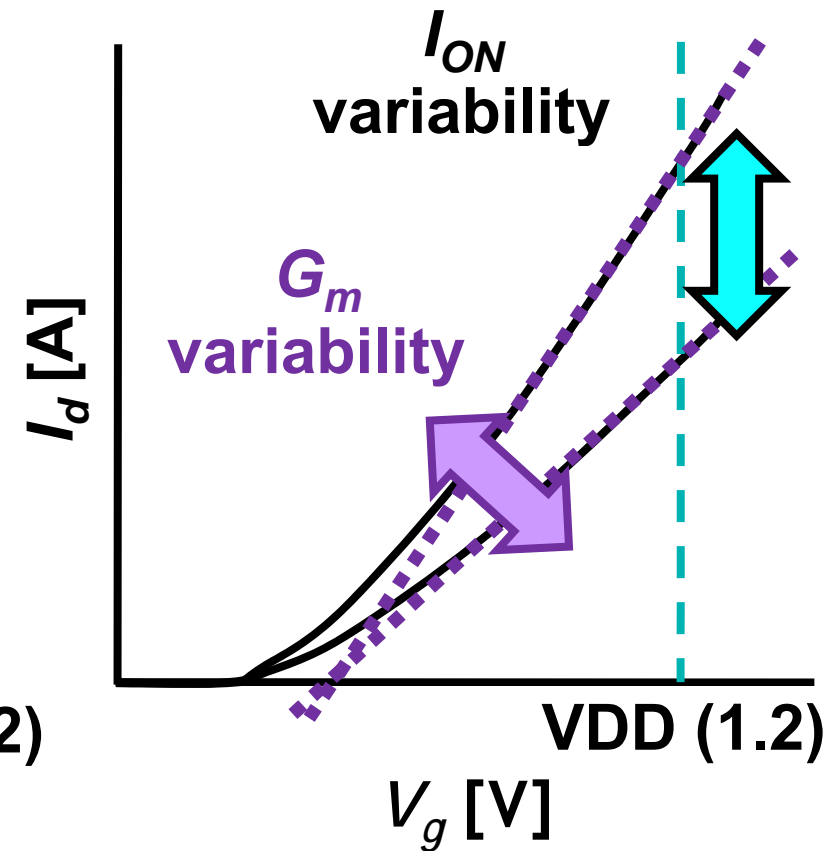
Drain Current Variability



Two Components (V_{thc} and g_m)

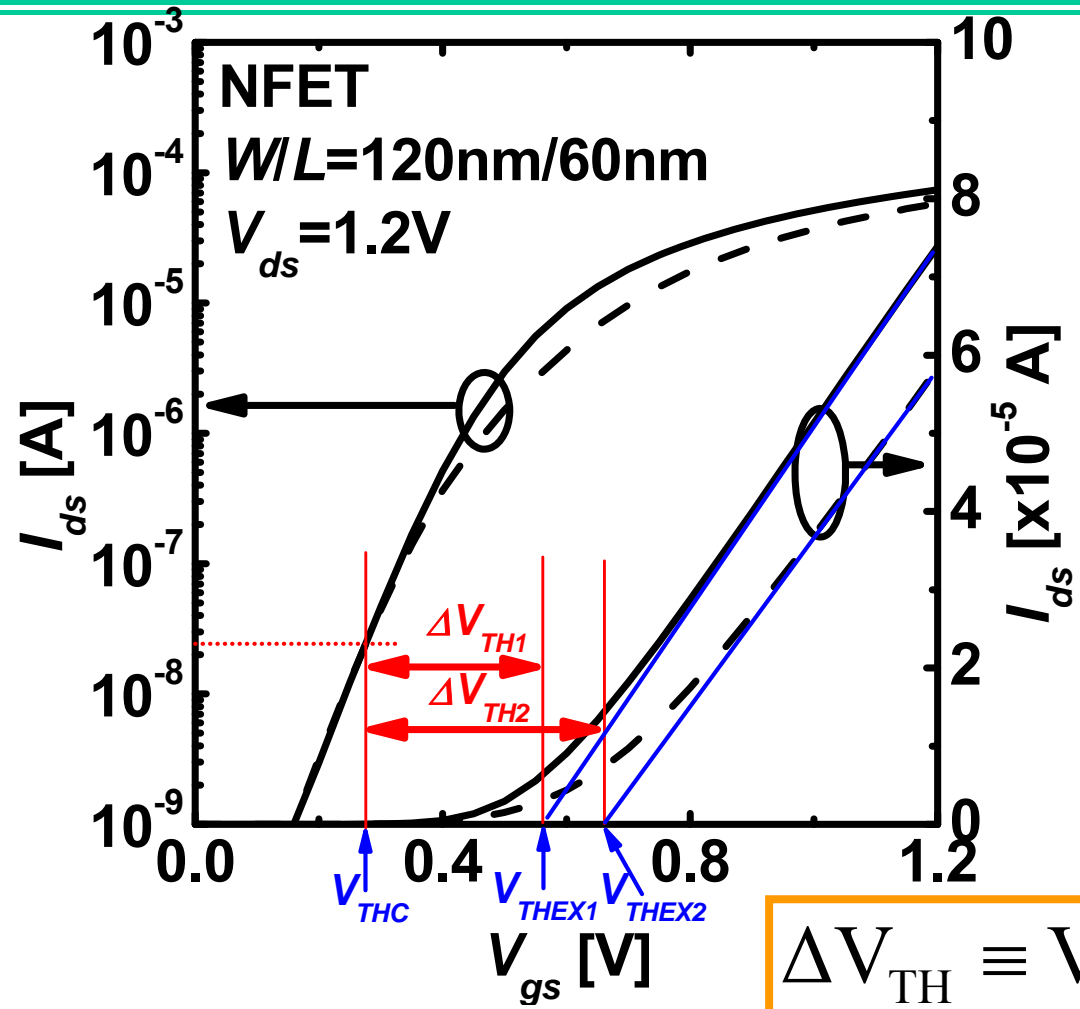


V_{THC} Component



G_m Component

Two Transistors with same V_{thc} and g_m



$$\Delta V_{TH} \equiv V_{THEX} - V_{THC}$$

T. Tsunomura et al., VLSI Technology Symposium, p. 97, 2010.

“Current-Onset Voltage”
 9

Definition of Current Onset Voltage ΔV_{TH}

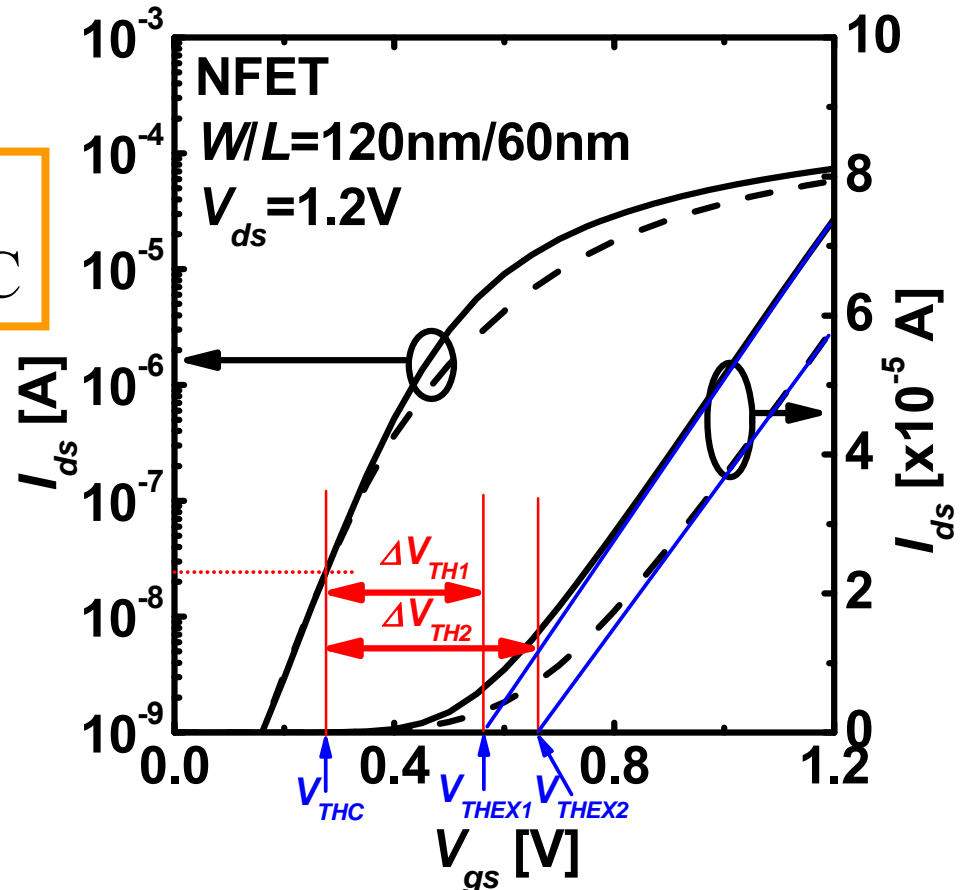
The 3rd Component of Drain Current Variability

“Current-Onset Voltage”

$$\Delta V_{TH} \equiv V_{THEX} - V_{THC}$$

Extrapolated V_{th}

Subthreshold Constant Current V_{th}



Independent Three Components

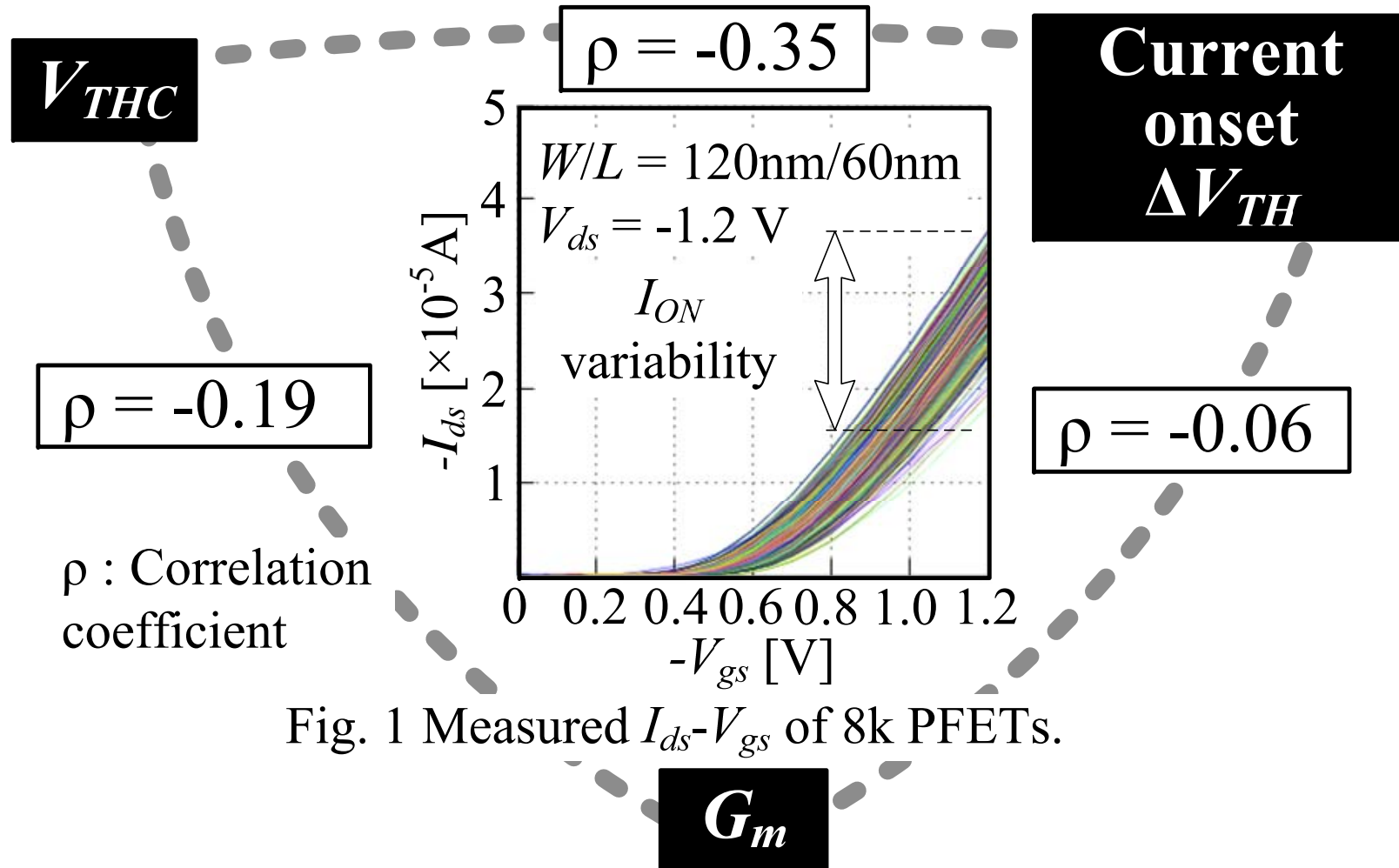
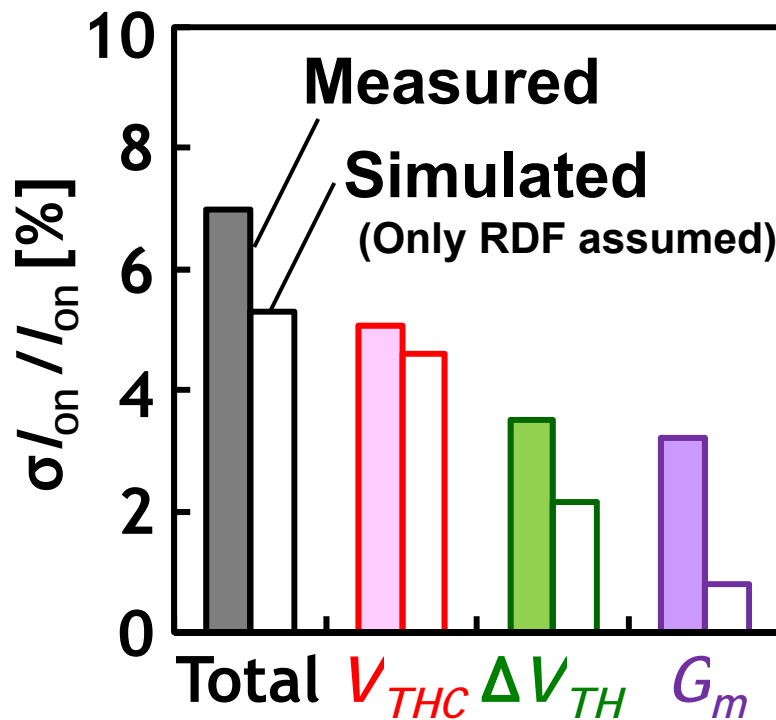


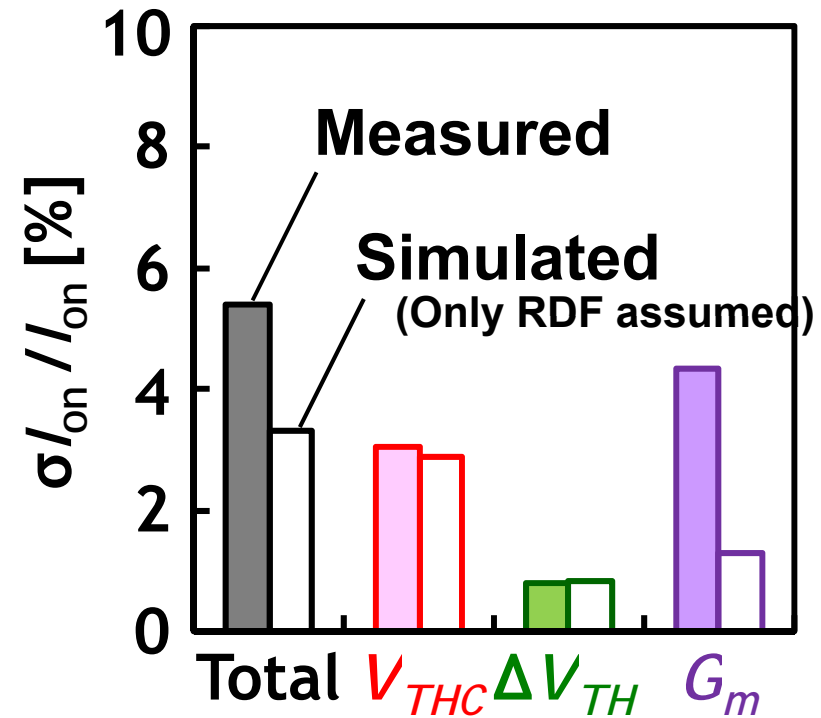
Fig. 1 Measured I_{ds} - V_{gs} of 8k PFETs.

Contributions of Three Components

PFET



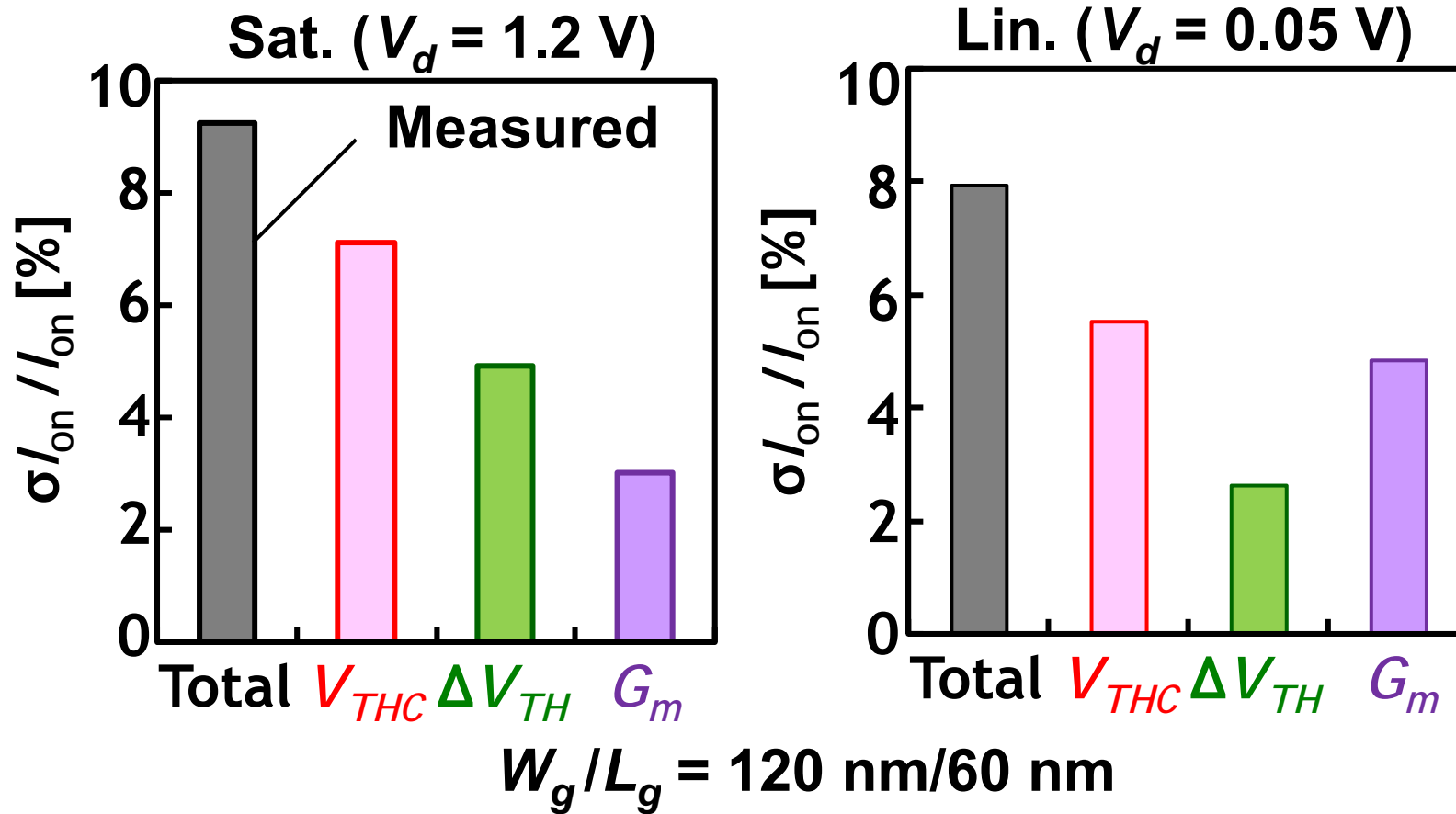
$W_g/L_g = 120 \text{ nm}/60 \text{ nm}$,
 $V_d = -1.2 \text{ V}$



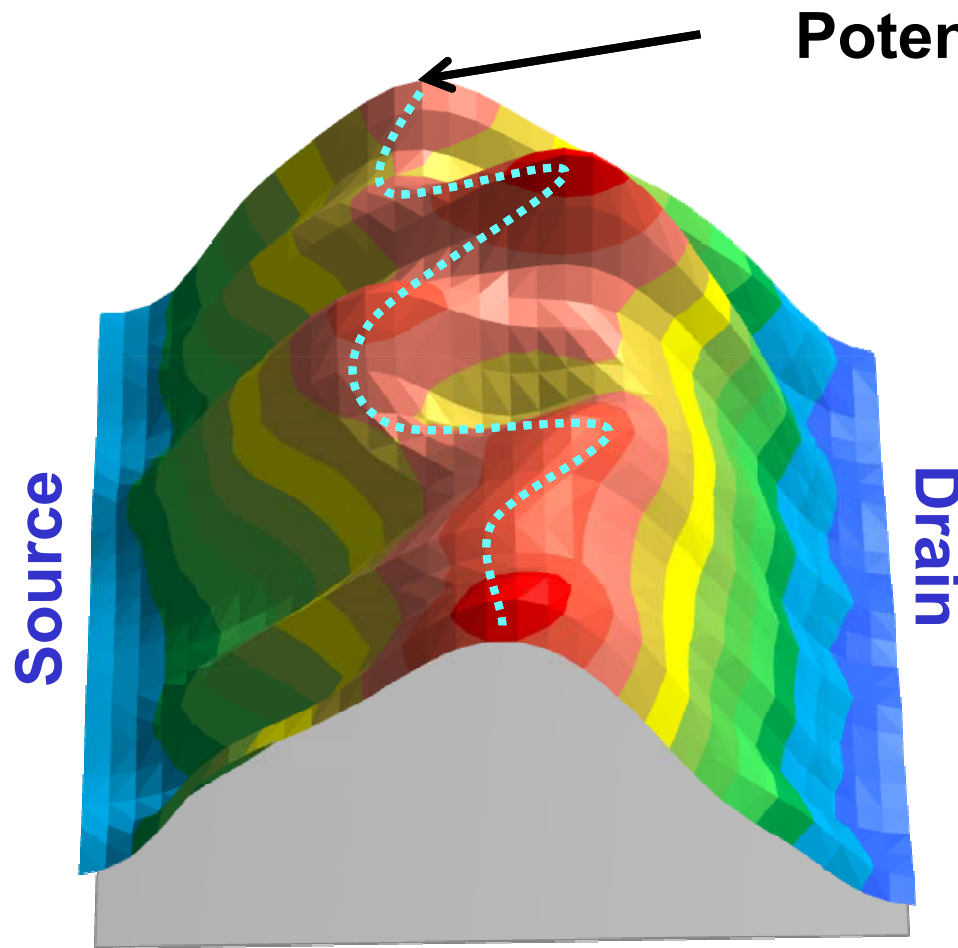
$W_g/L_g = 120 \text{ nm}/60 \text{ nm}$,
 $V_d = -0.05 \text{ V}$

Contributions of Three Components

NFET



The Origin of ΔV_{TH}

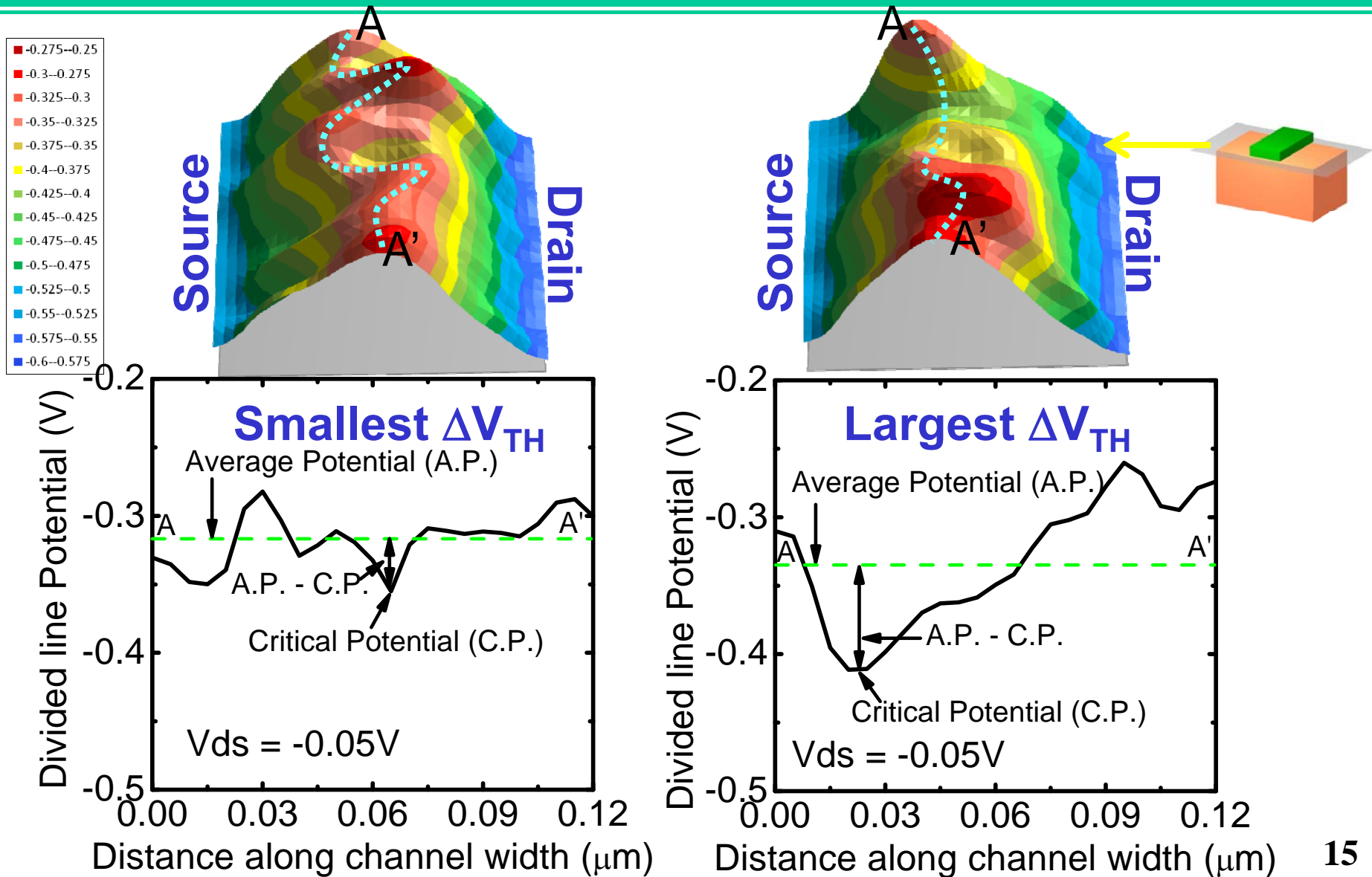


Potential Divided line

V_{THC} : Subthreshold region
Determined by the
minimum potential on
the divided line?

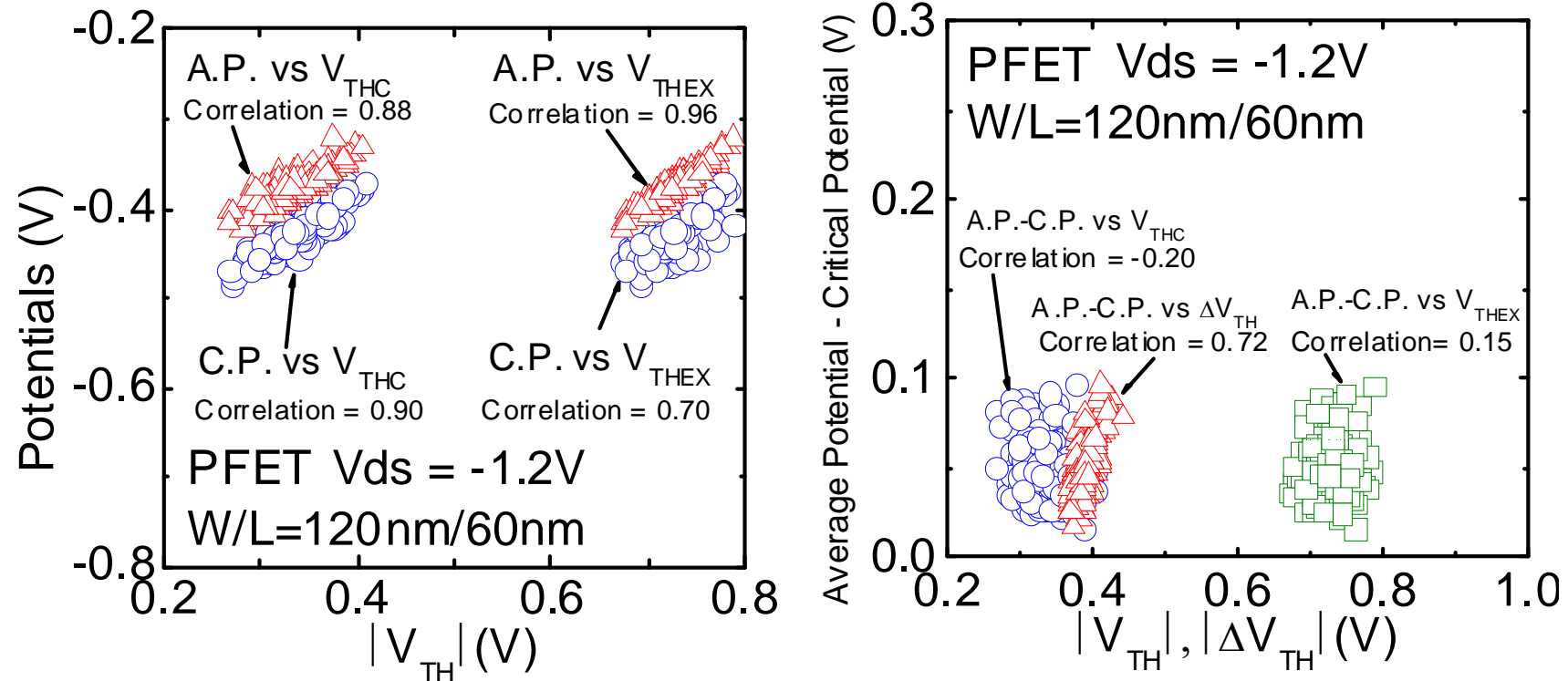
V_{THEX} : Strong inversion
Average potential?

Simulated Potential Profile



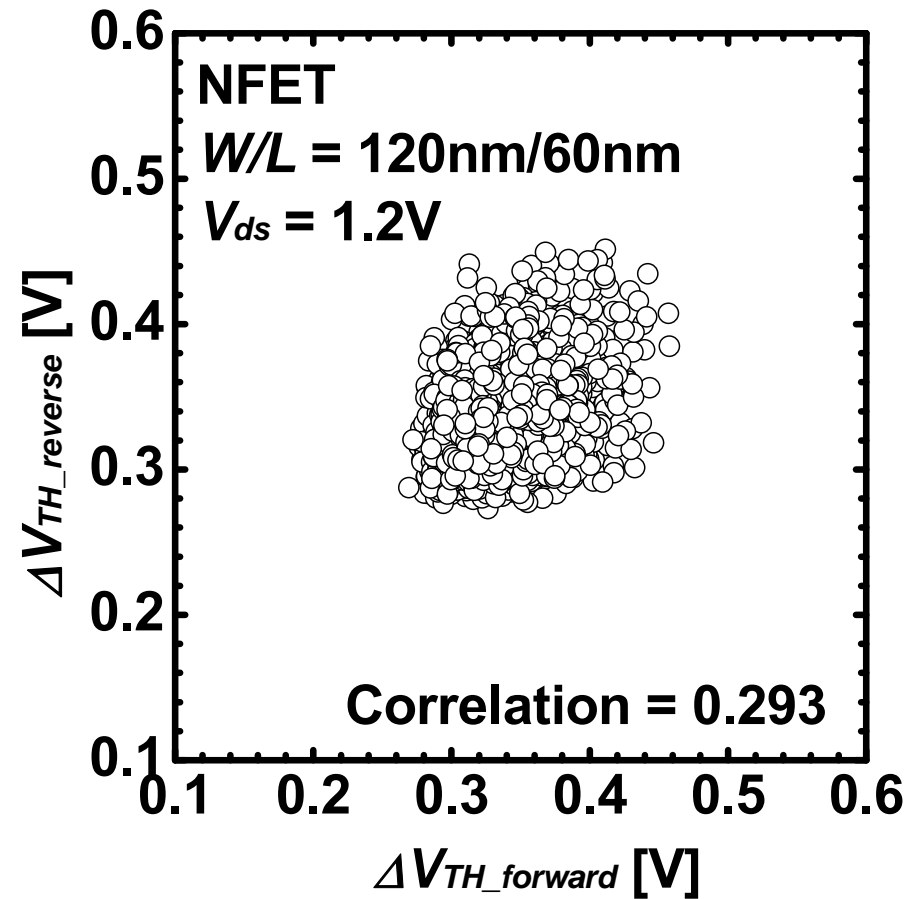
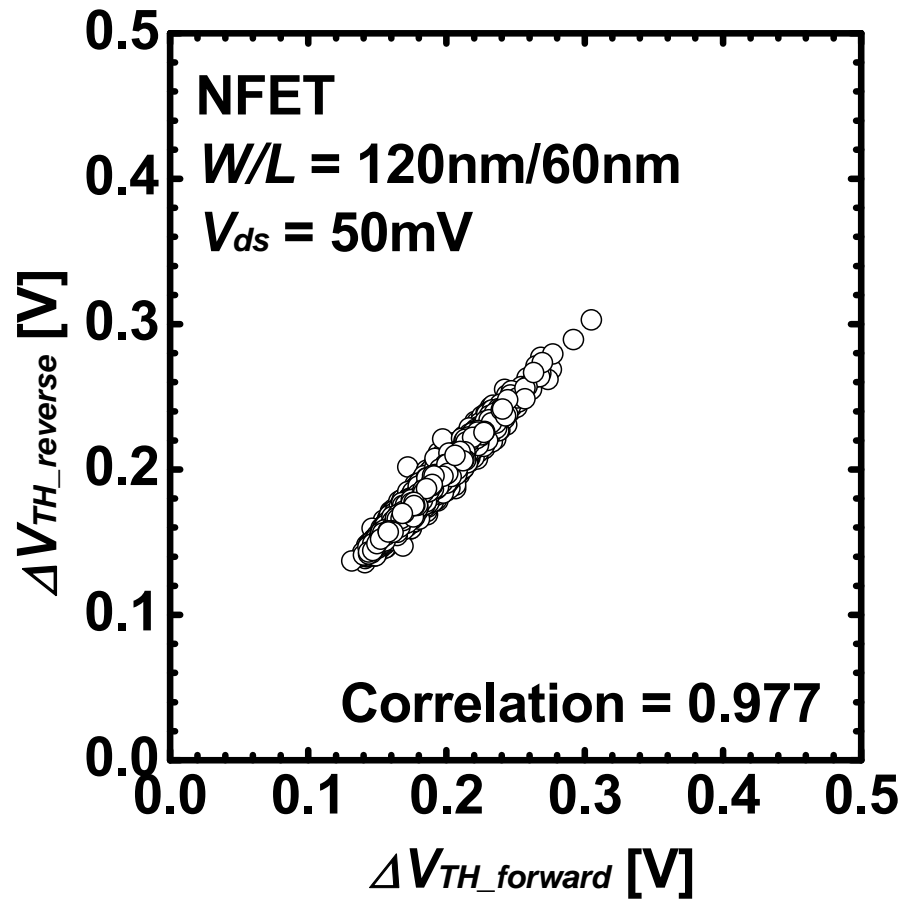
Correlation between ΔV_{TH} and V_{TH} 's

Simulation



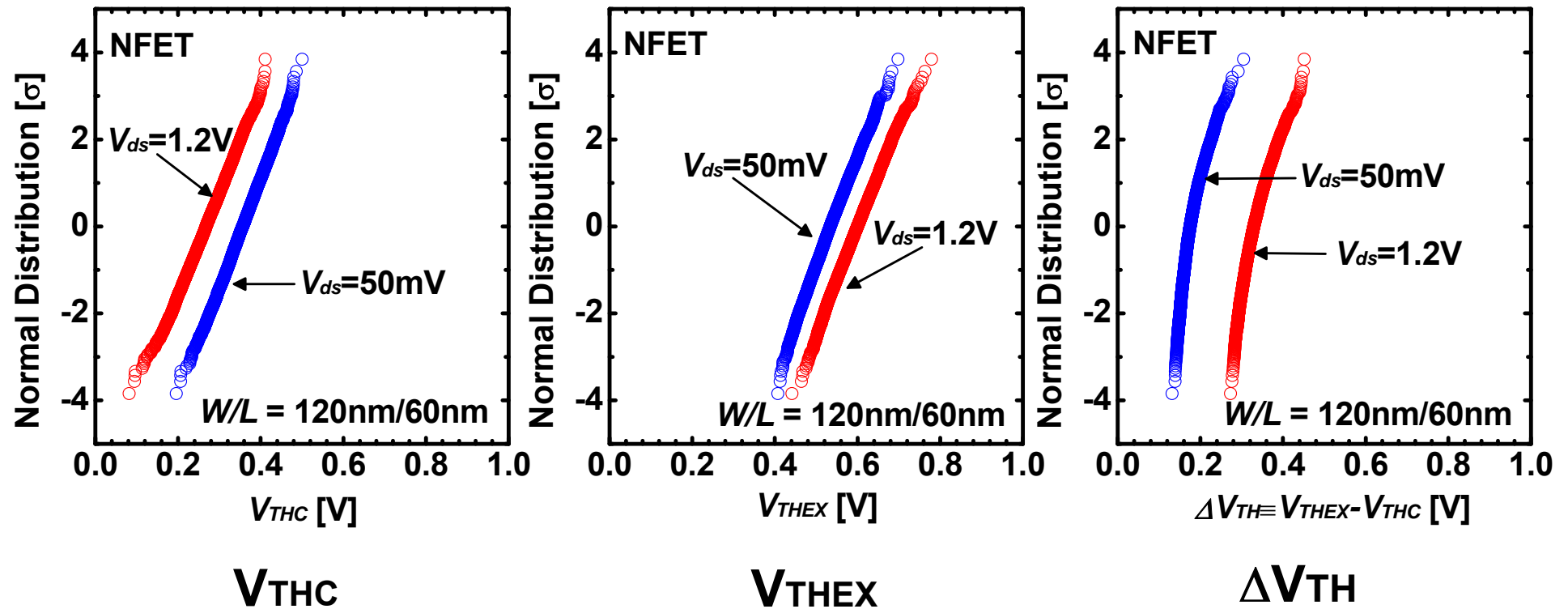
Reversed S/D

Measurement

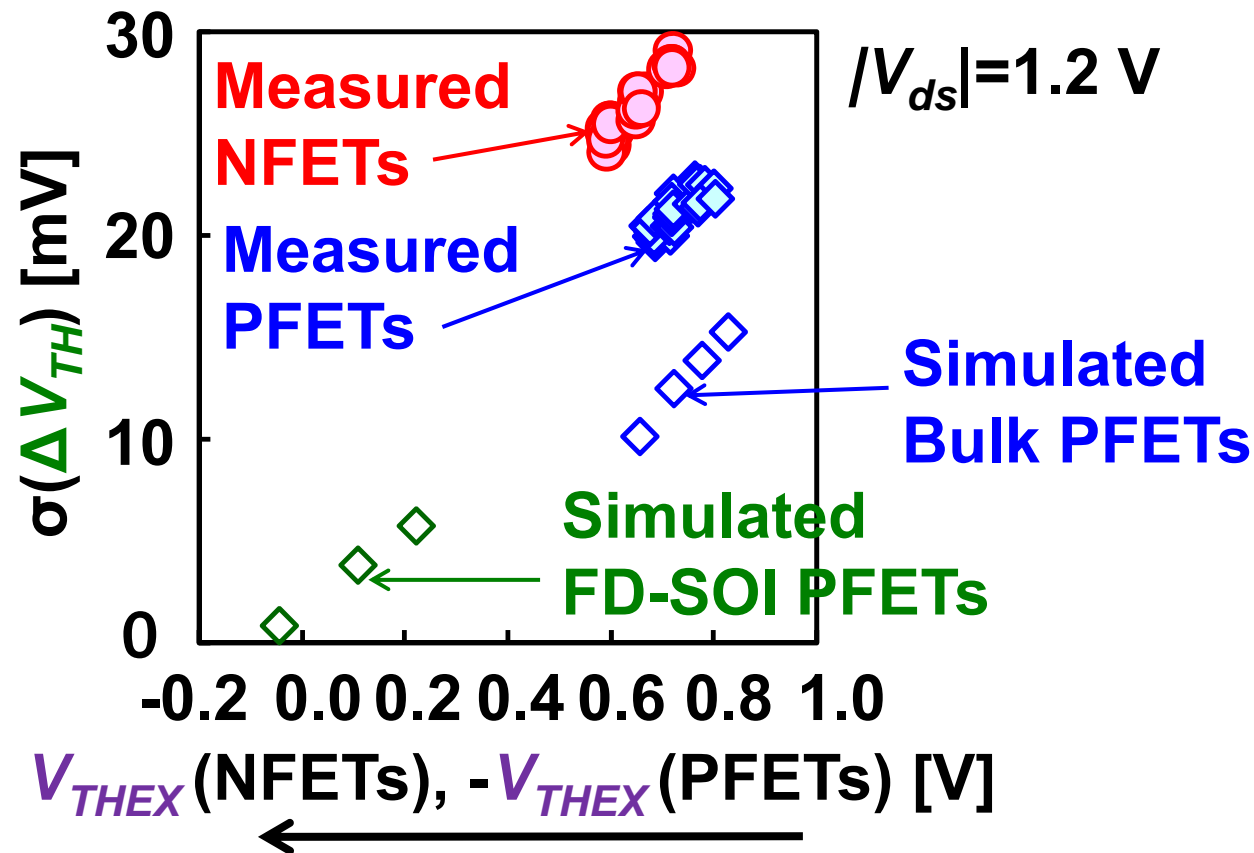


Cumulative Distribution

Measurement

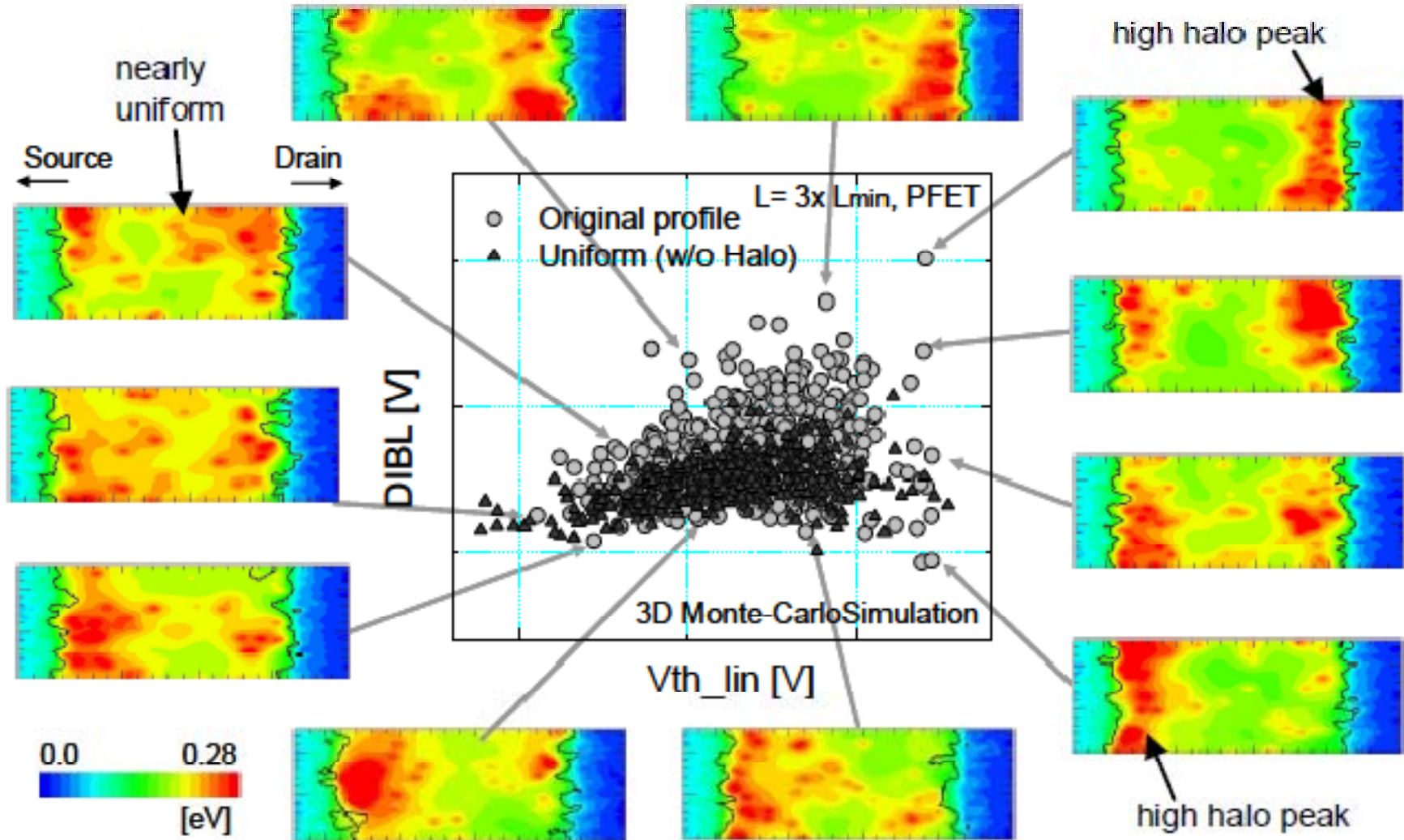


Dopant Density v.s. $\sigma(\Delta V_{TH})$

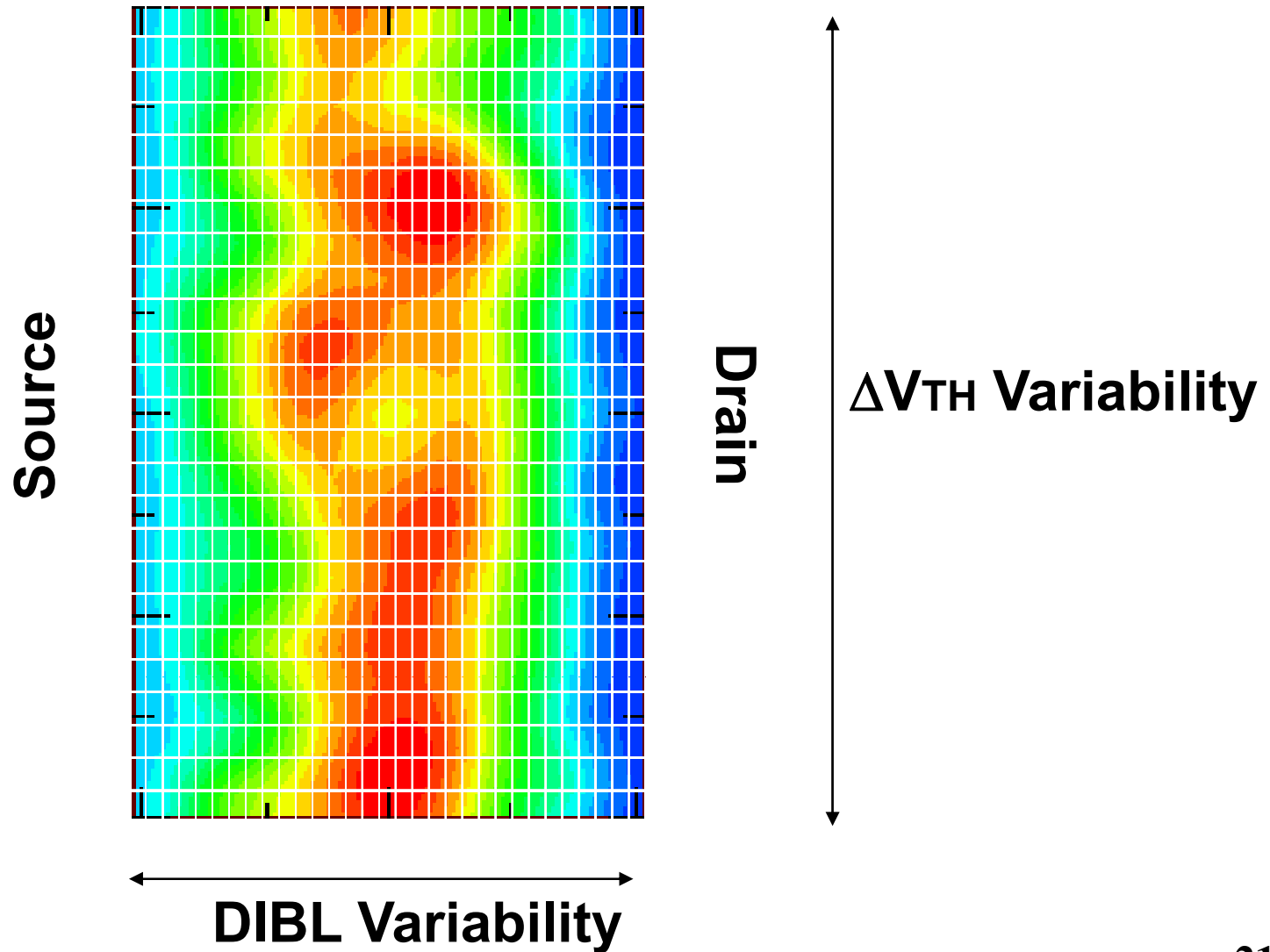


- V_{THEX} is controlled by the channel dopant concentration.

DIBL and Potential Profile

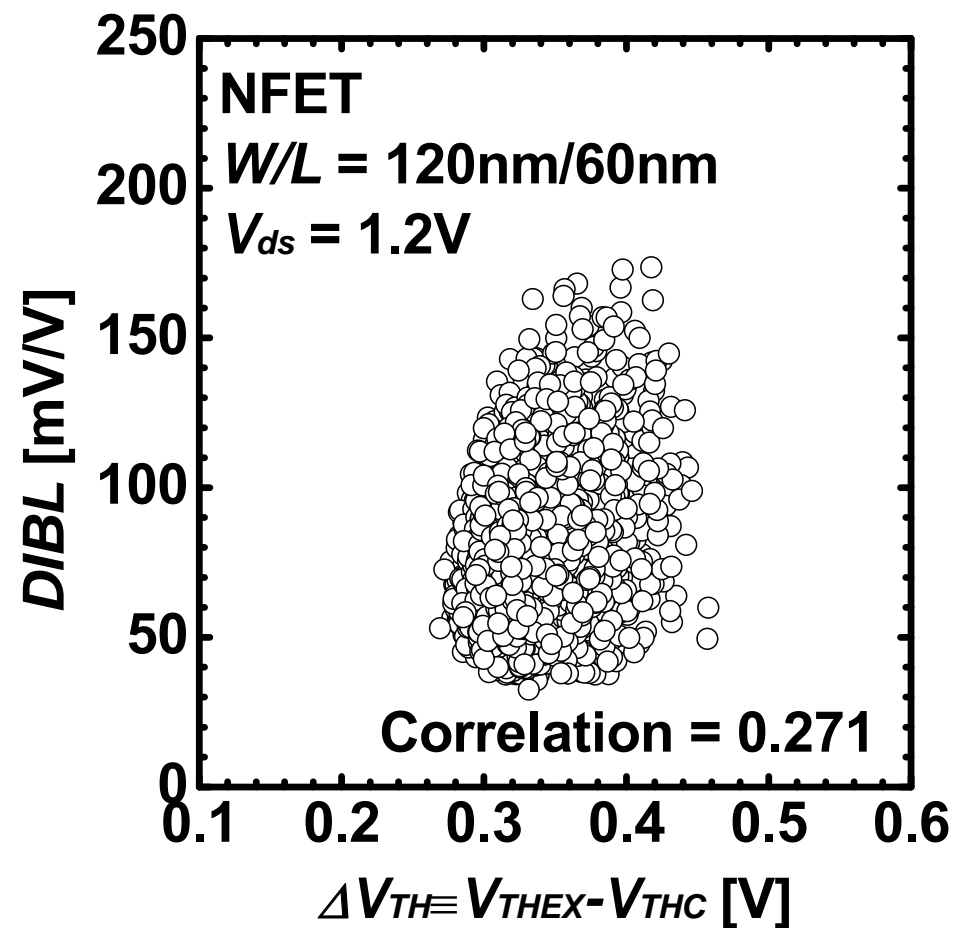
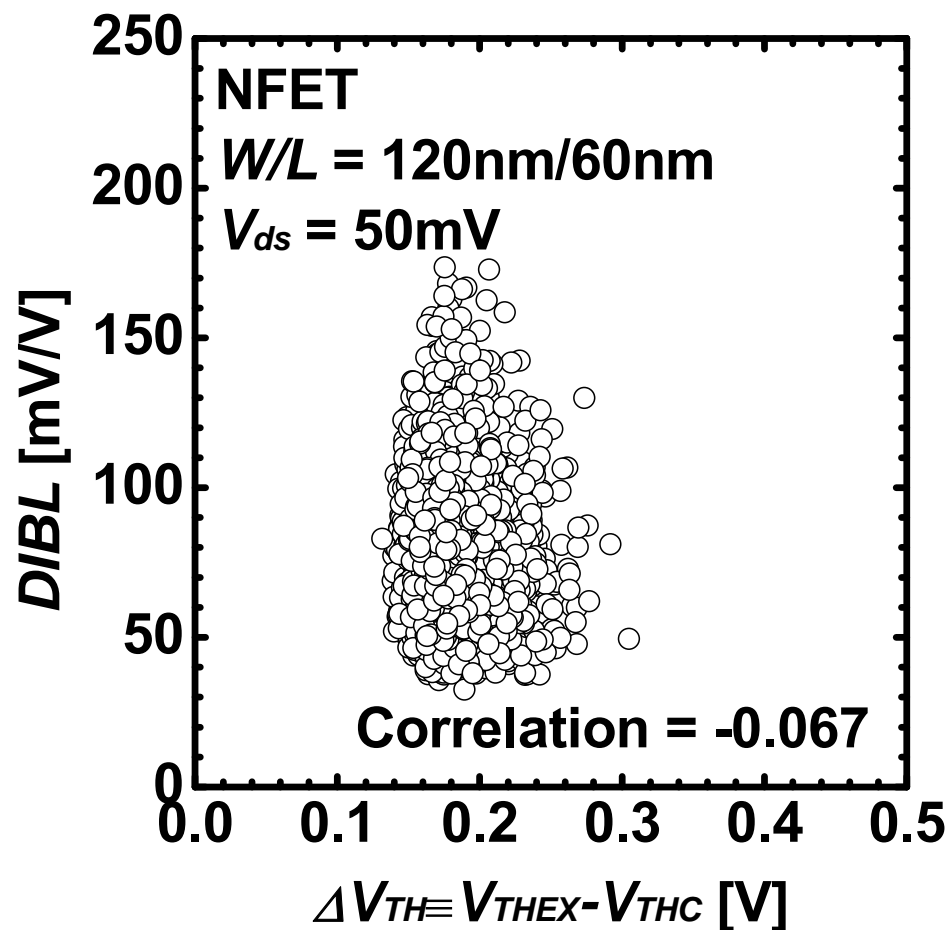


ΔV_{TH} Variability and DIBL Variability



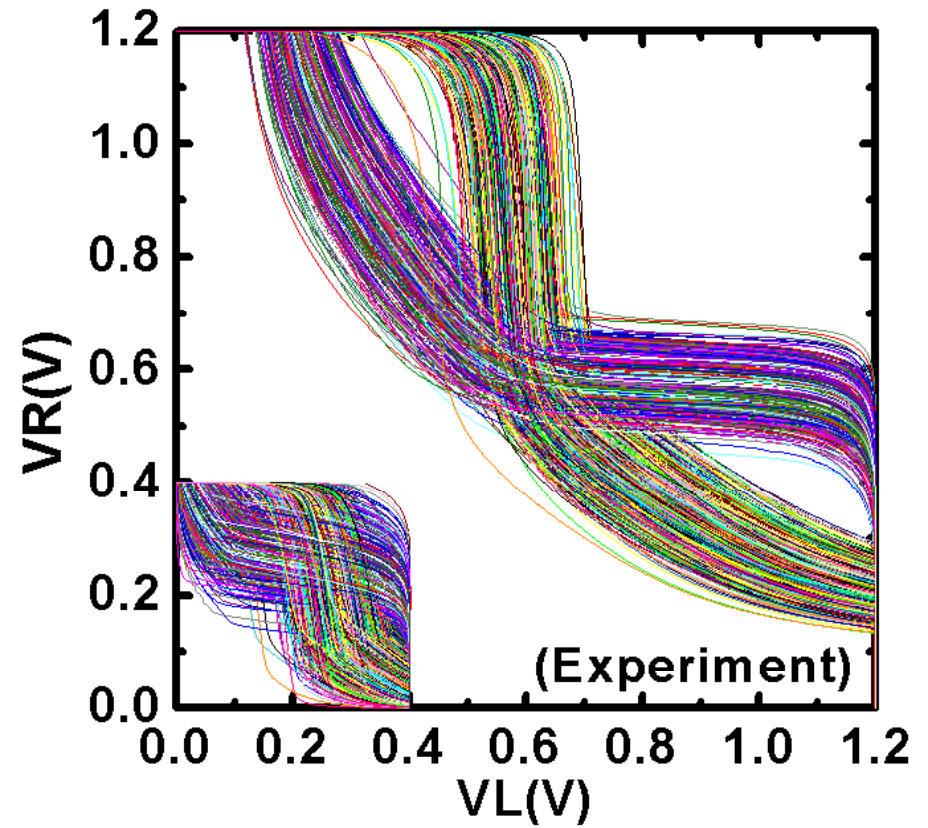
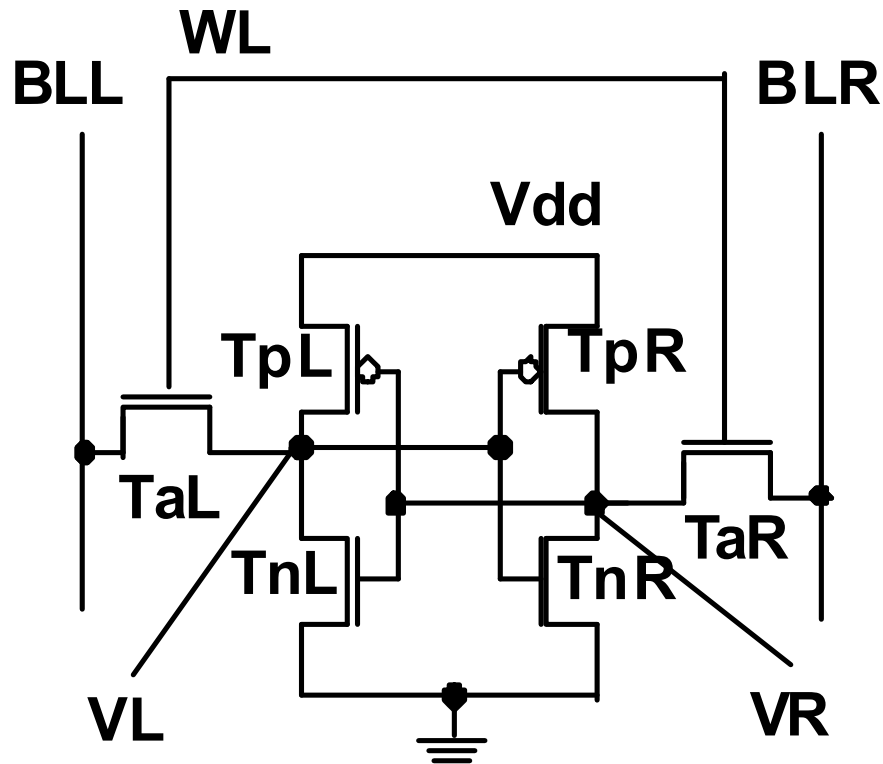
Correlation between ΔV_{TH} and DIBL

Measurement

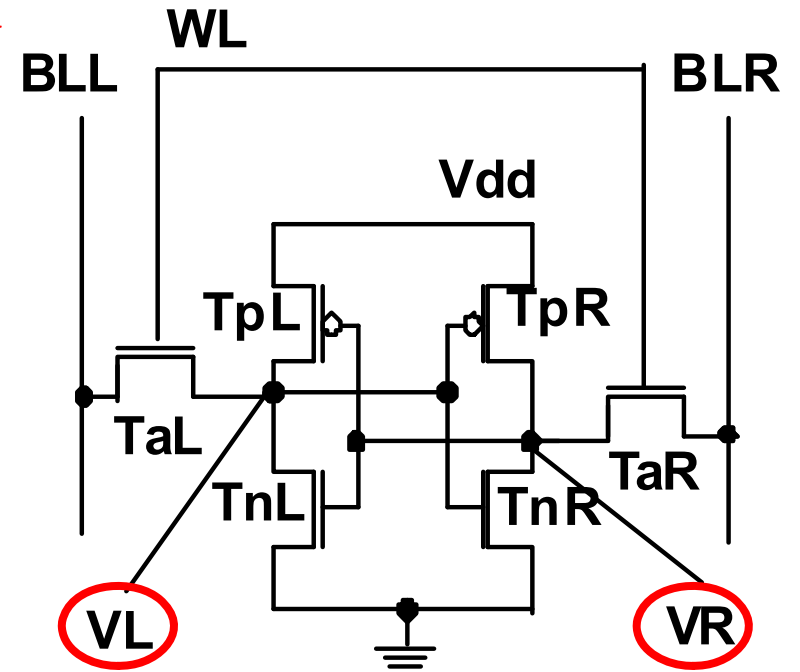
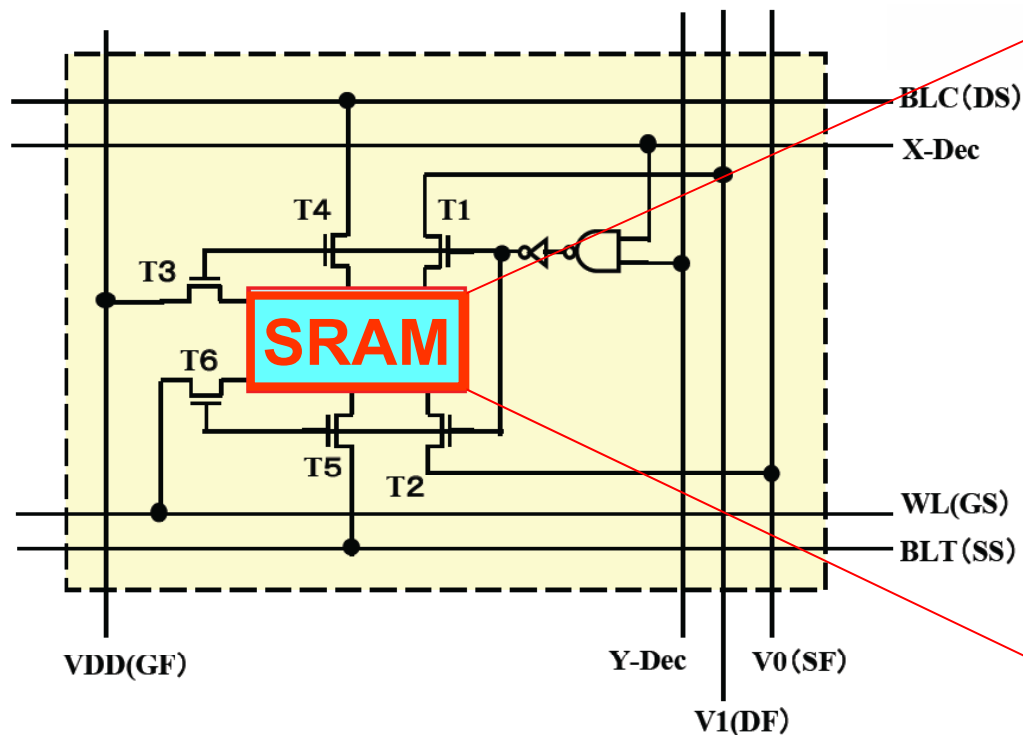


SRAM Variability

SRAM

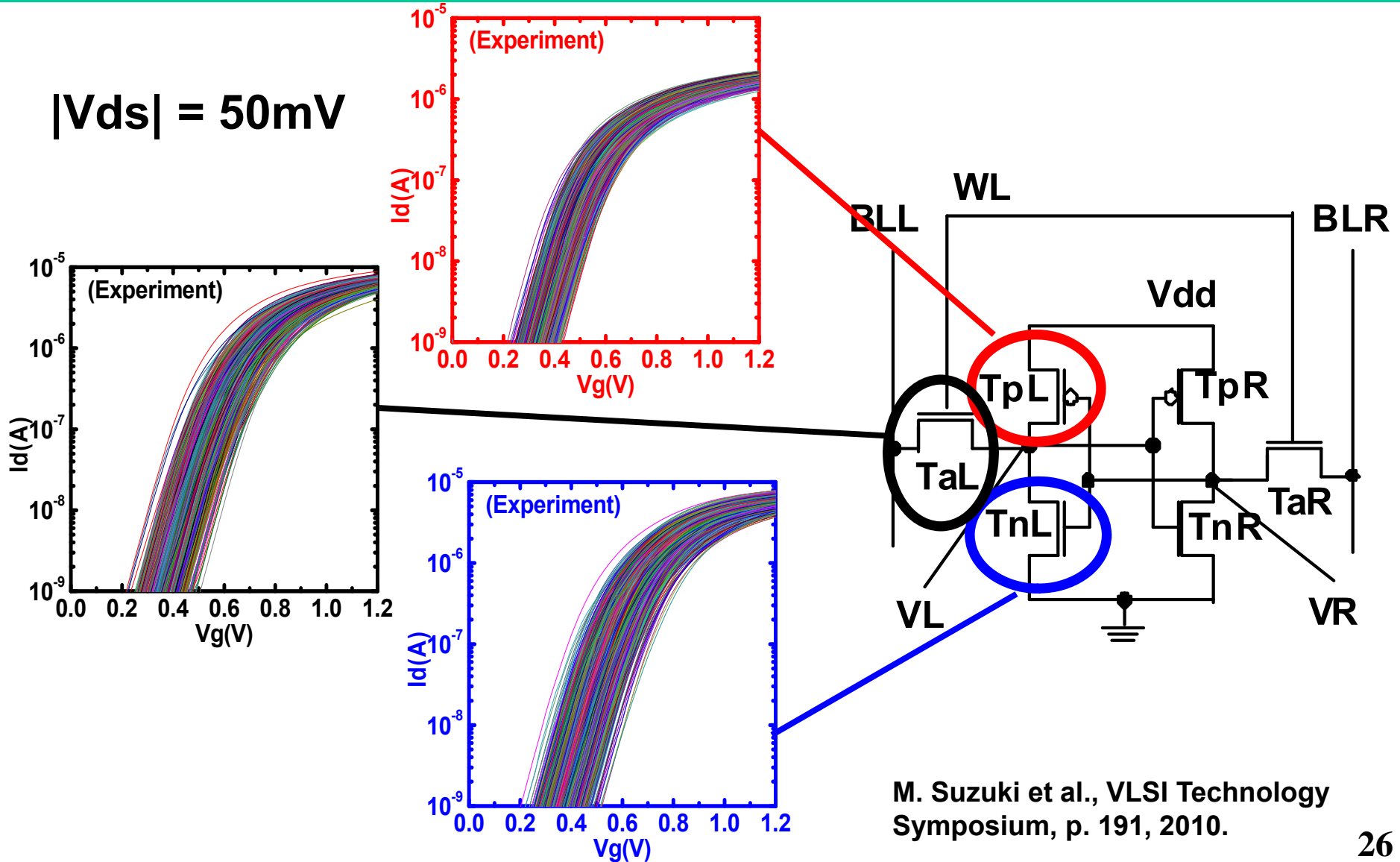


16k SRAM DMA TEG



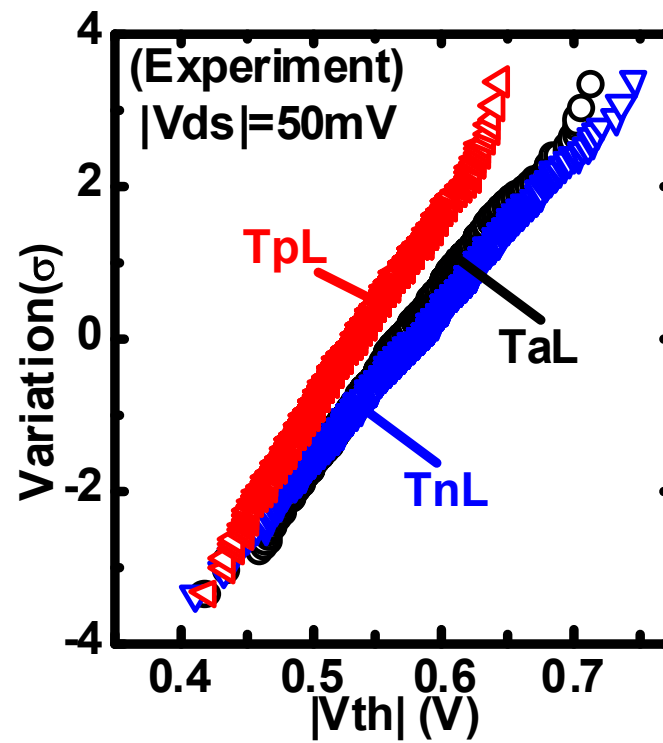
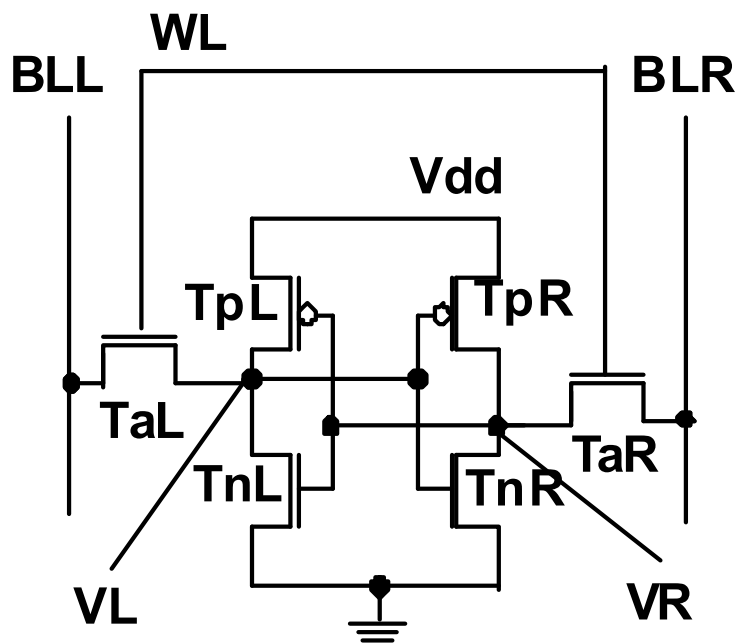
Measured I-V in Individual Transistors

$|V_{ds}| = 50\text{mV}$

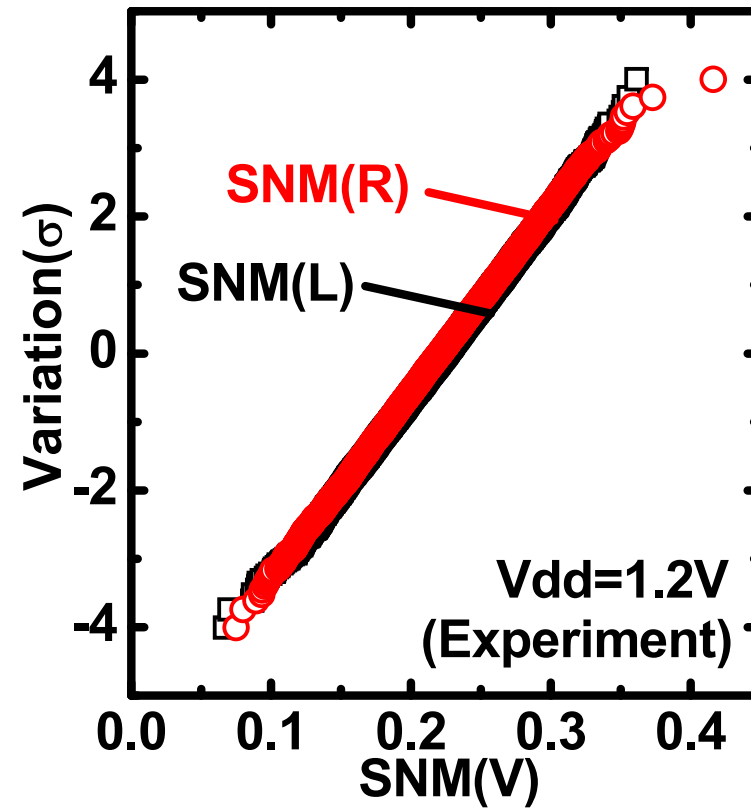
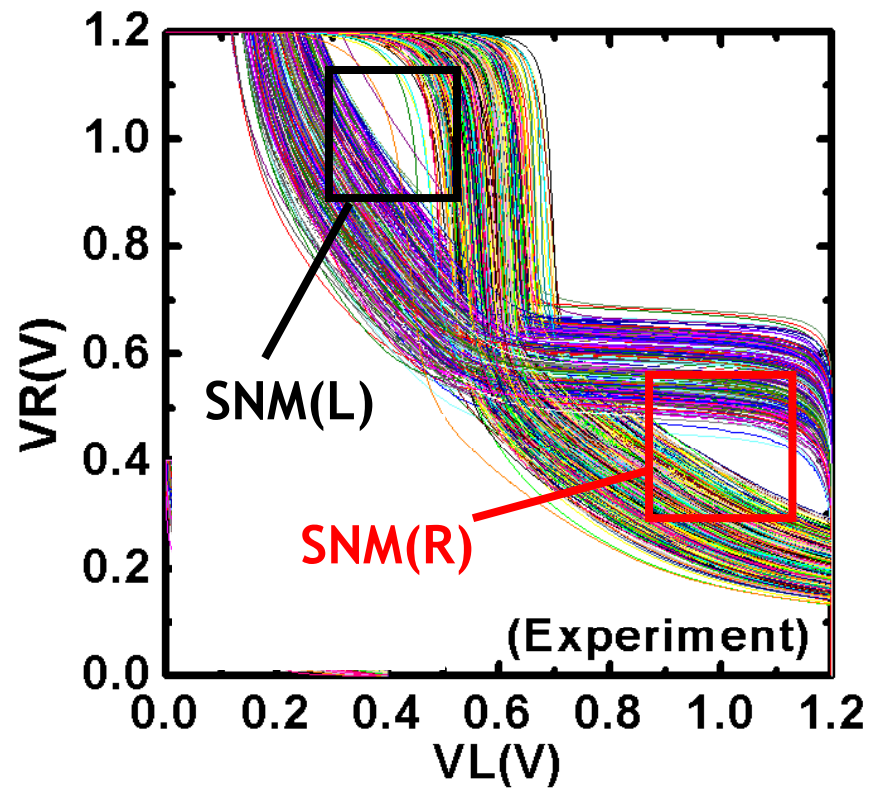


M. Suzuki et al., VLSI Technology Symposium, p. 191, 2010.

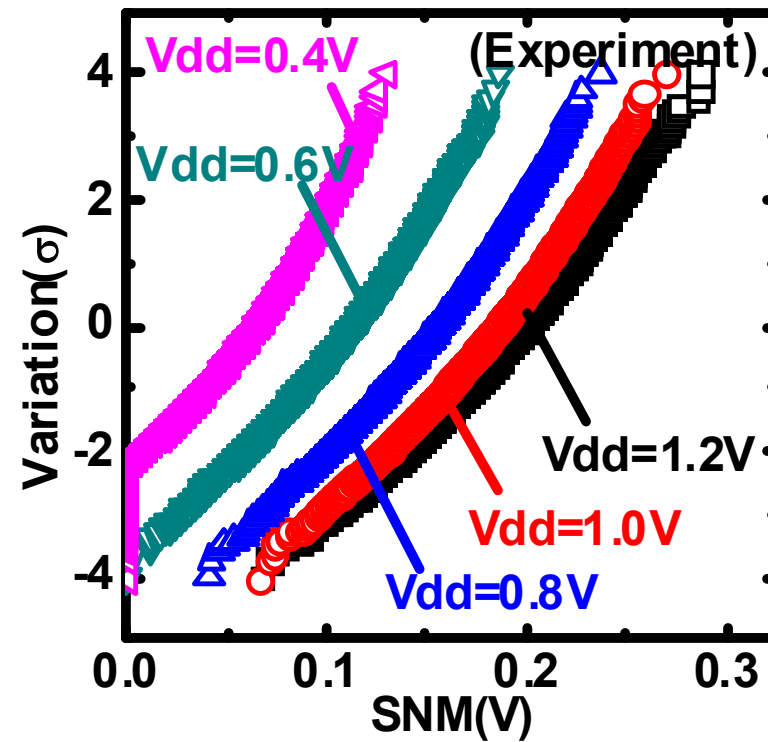
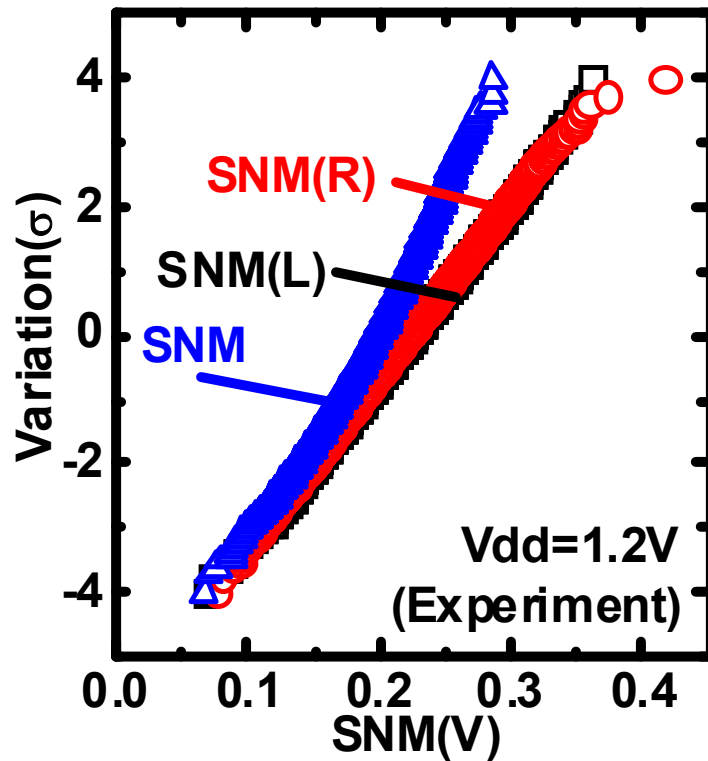
16k SRAM DMA TEG



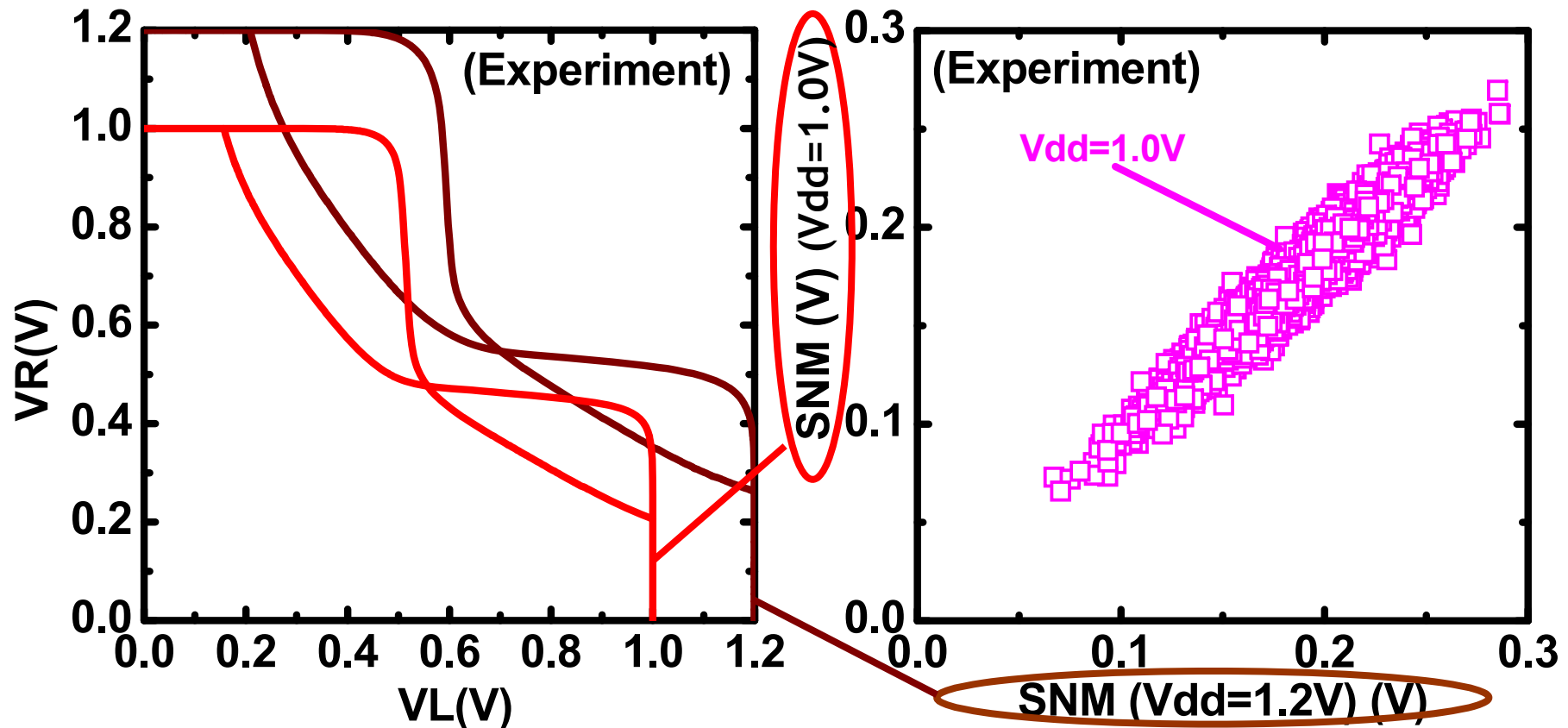
One-Side SNM



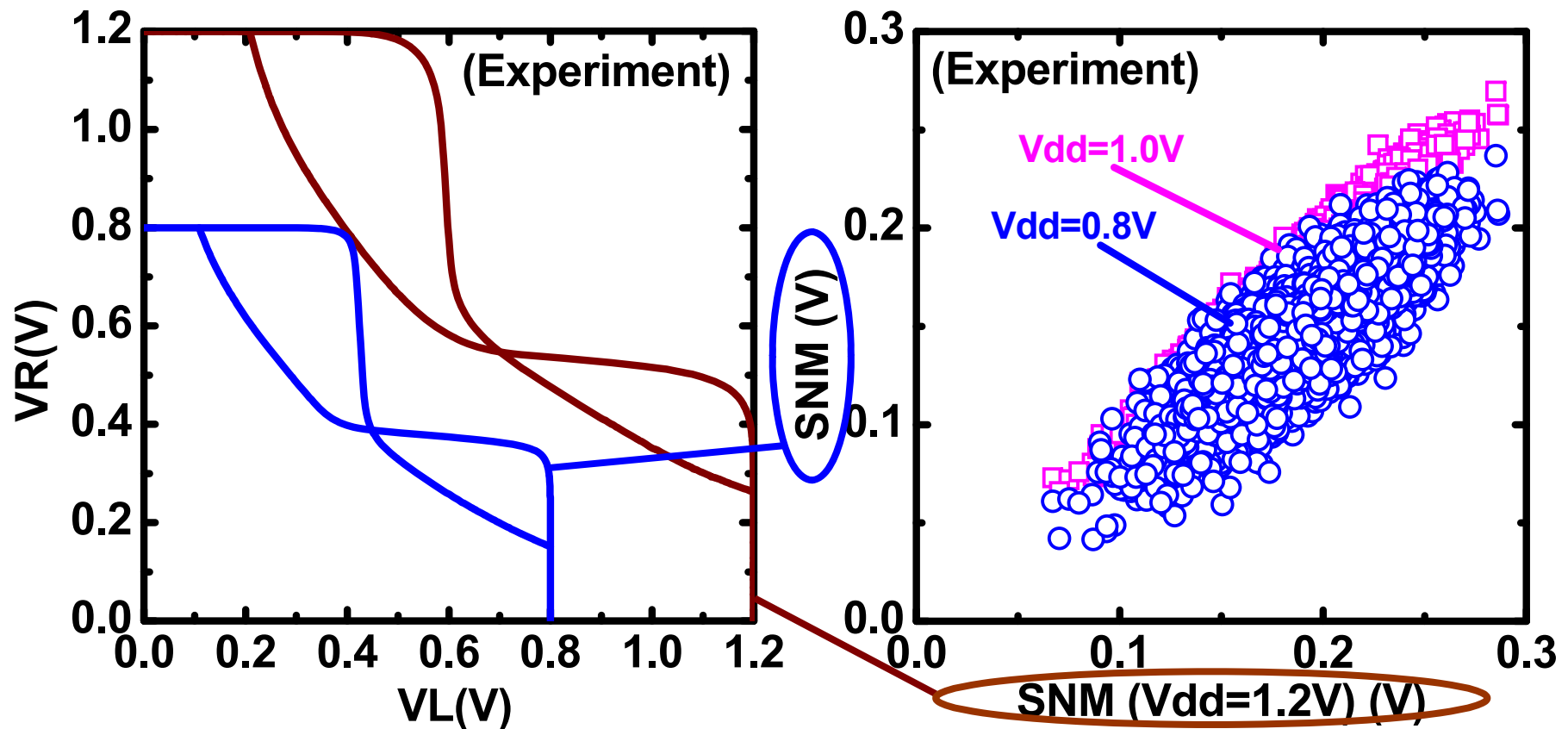
Distribution of SNM



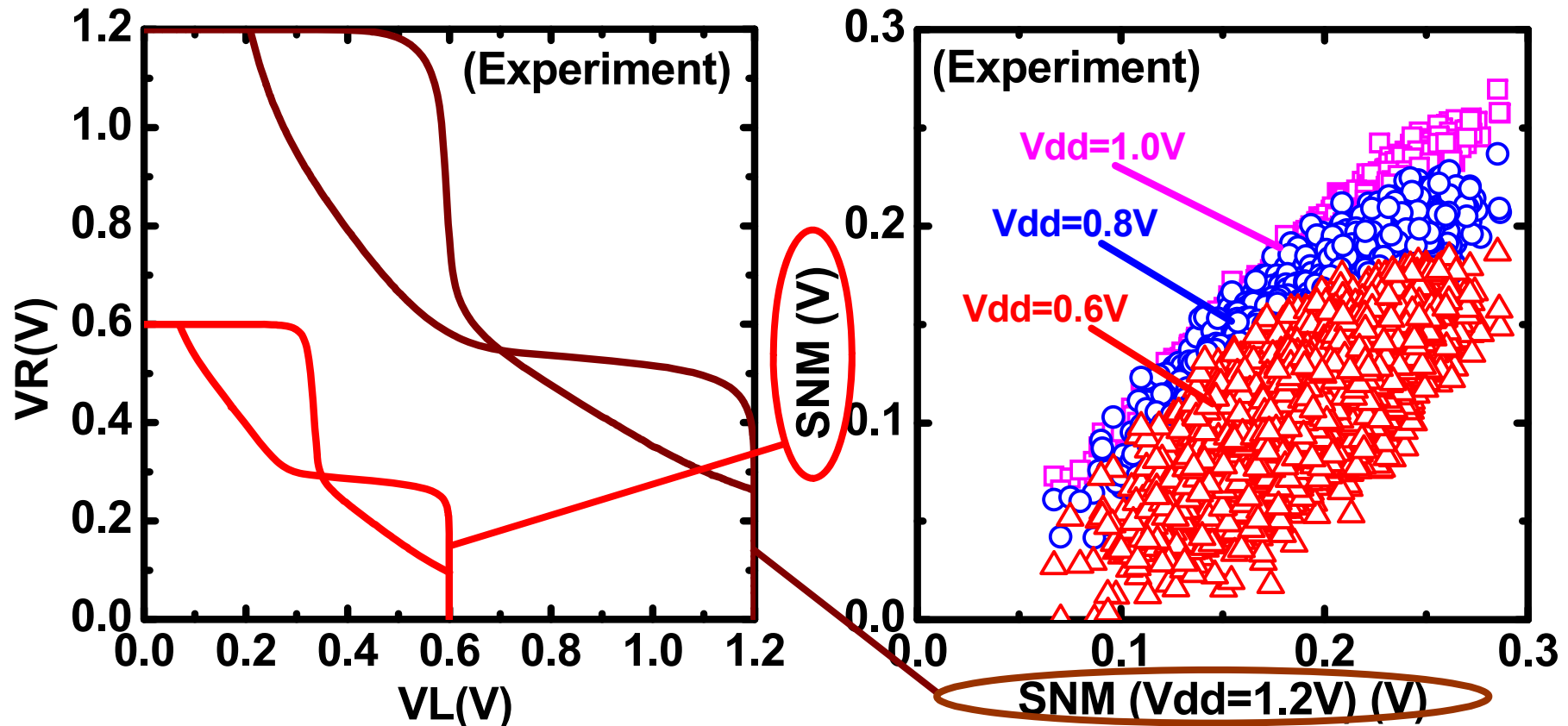
Correlation of SNM at Different Vdd



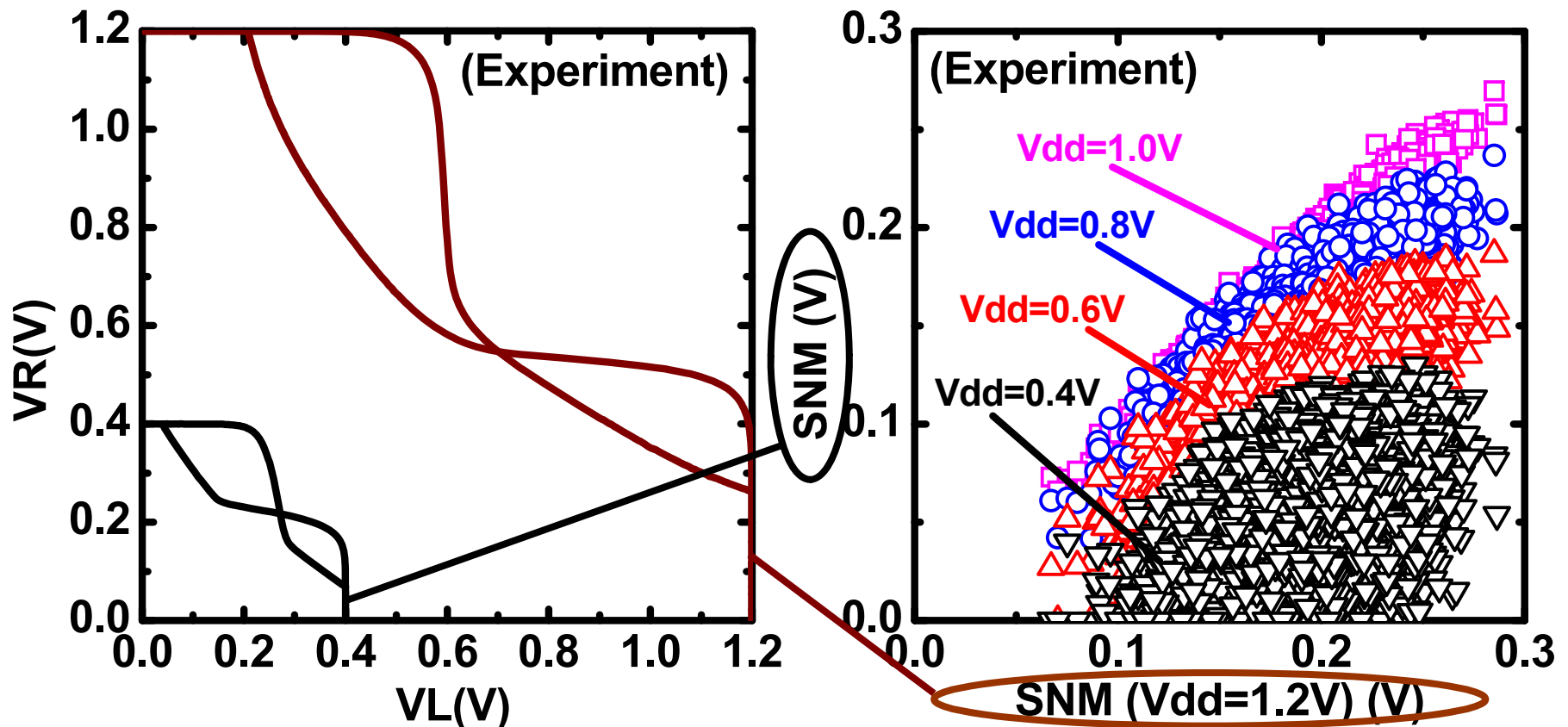
Correlation of SNM at Different Vdd



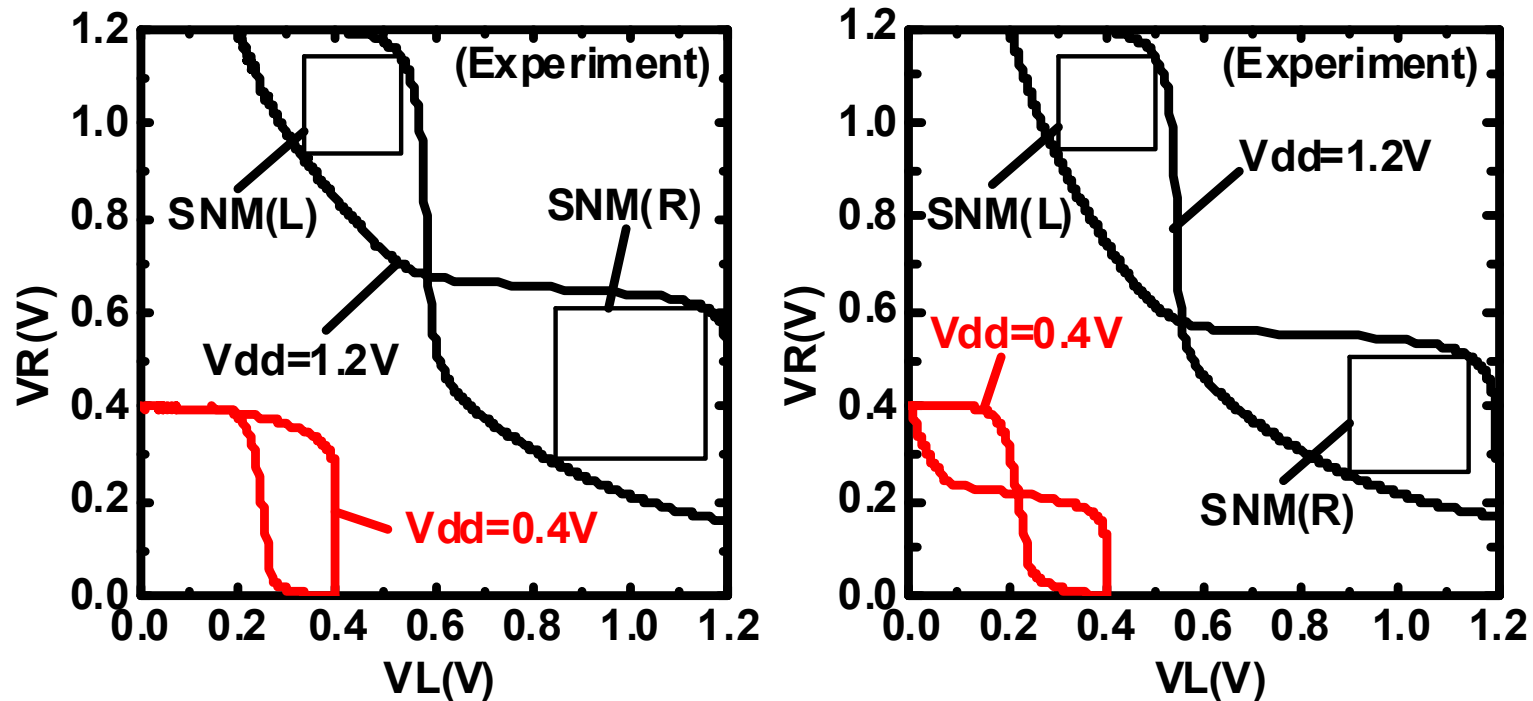
Correlation of SNM at Different Vdd



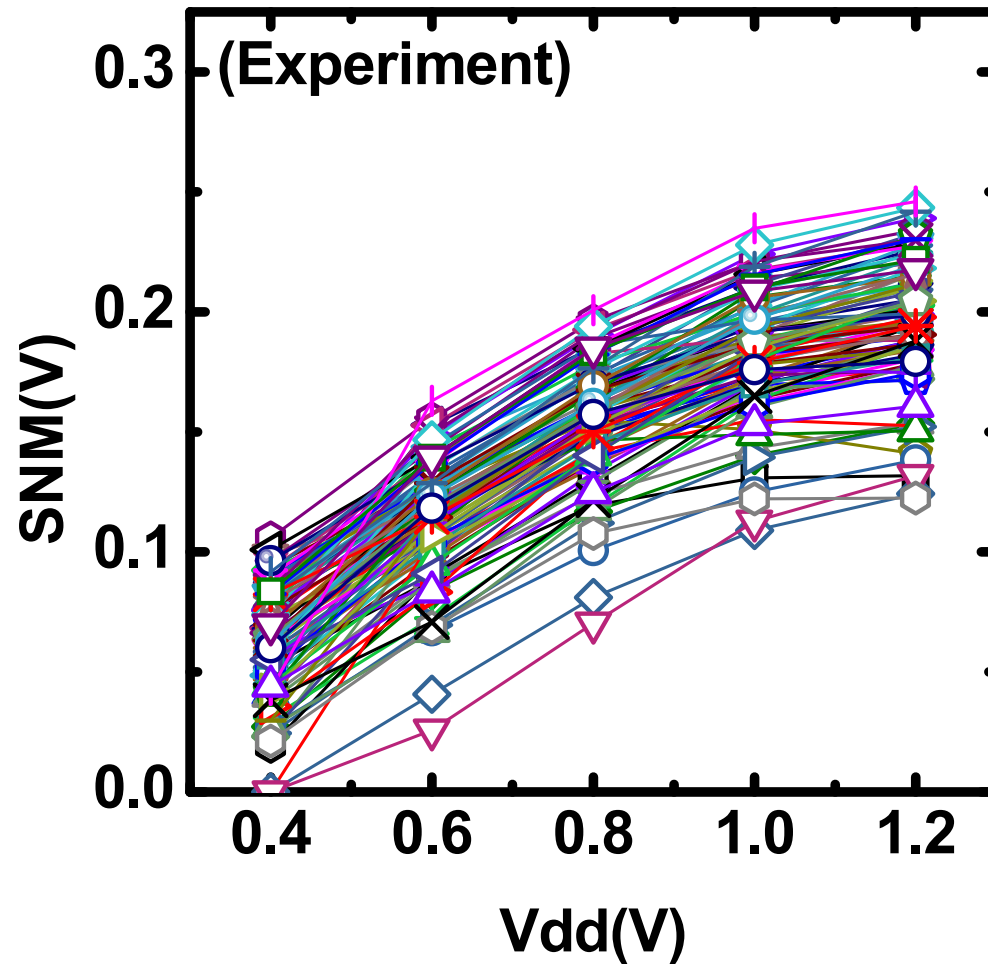
Correlation of SNM at Different Vdd



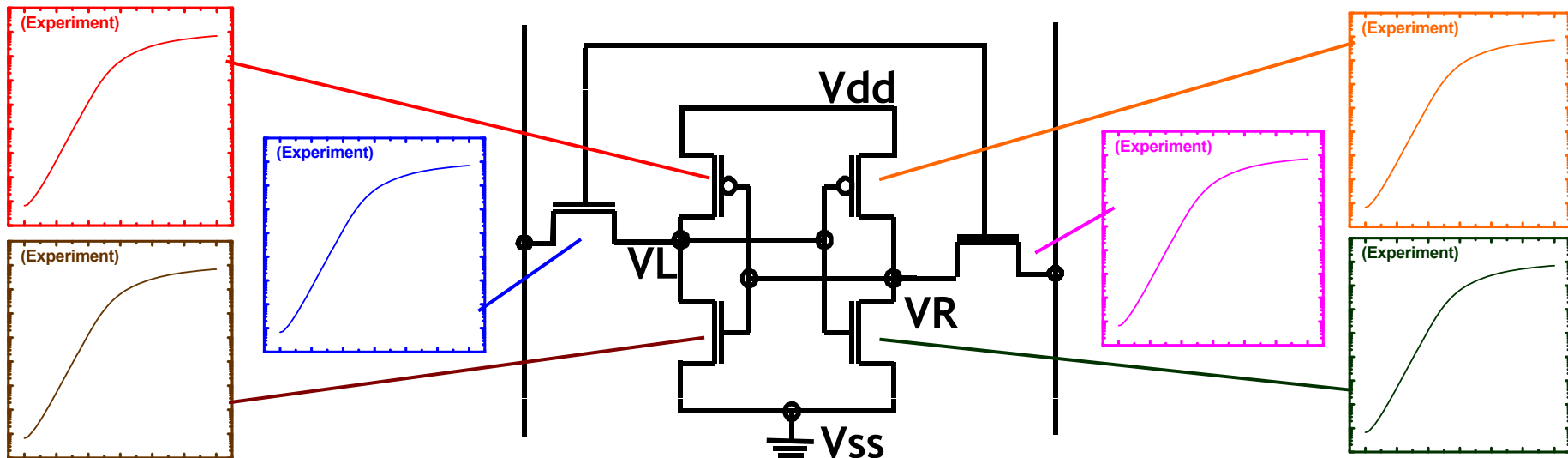
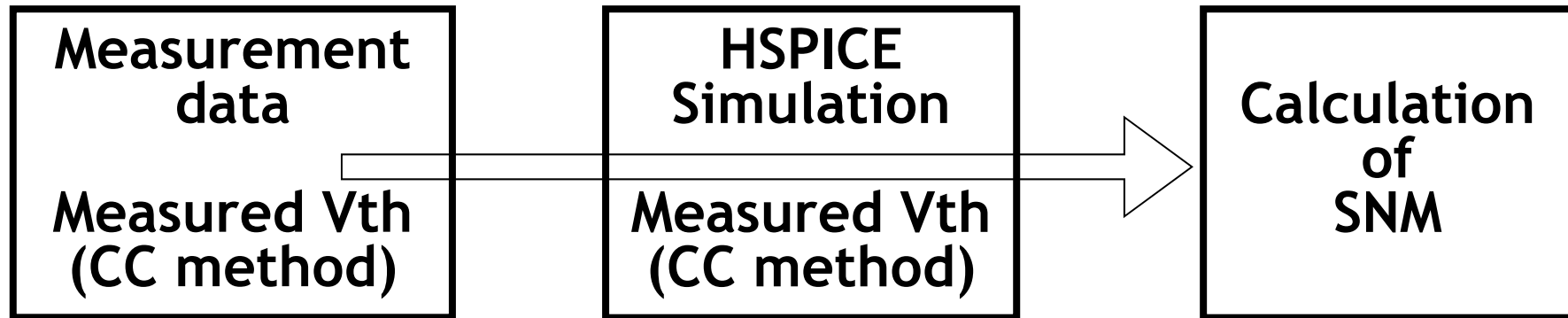
Two Cells with the Same SNM at 1.2V



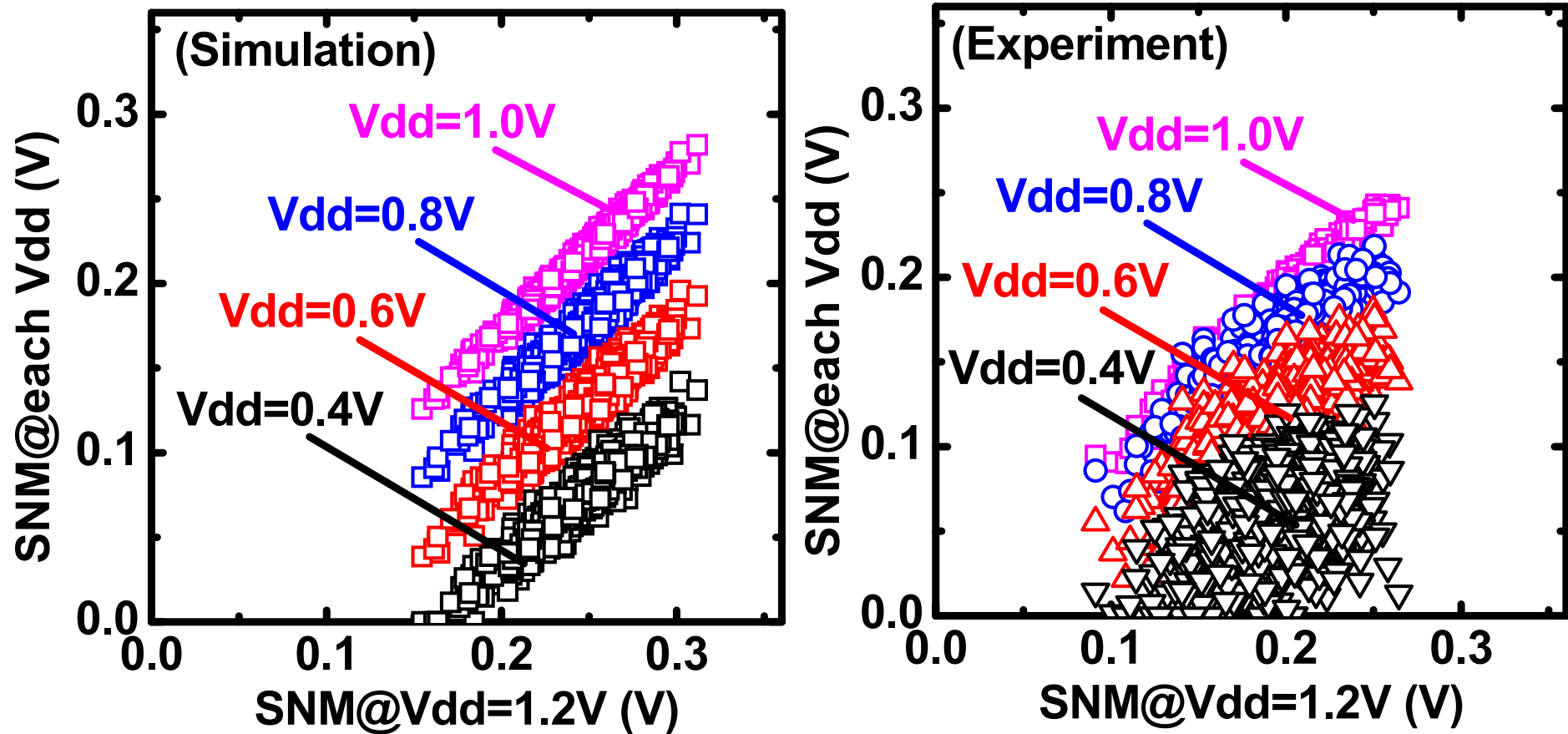
Vdd Dependence of SNM



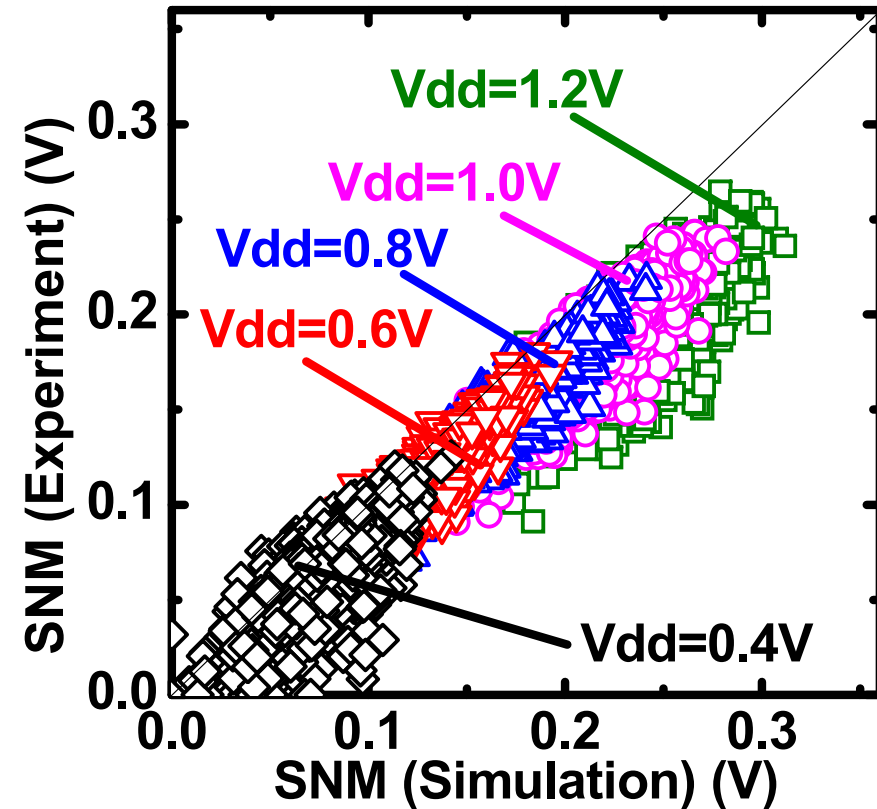
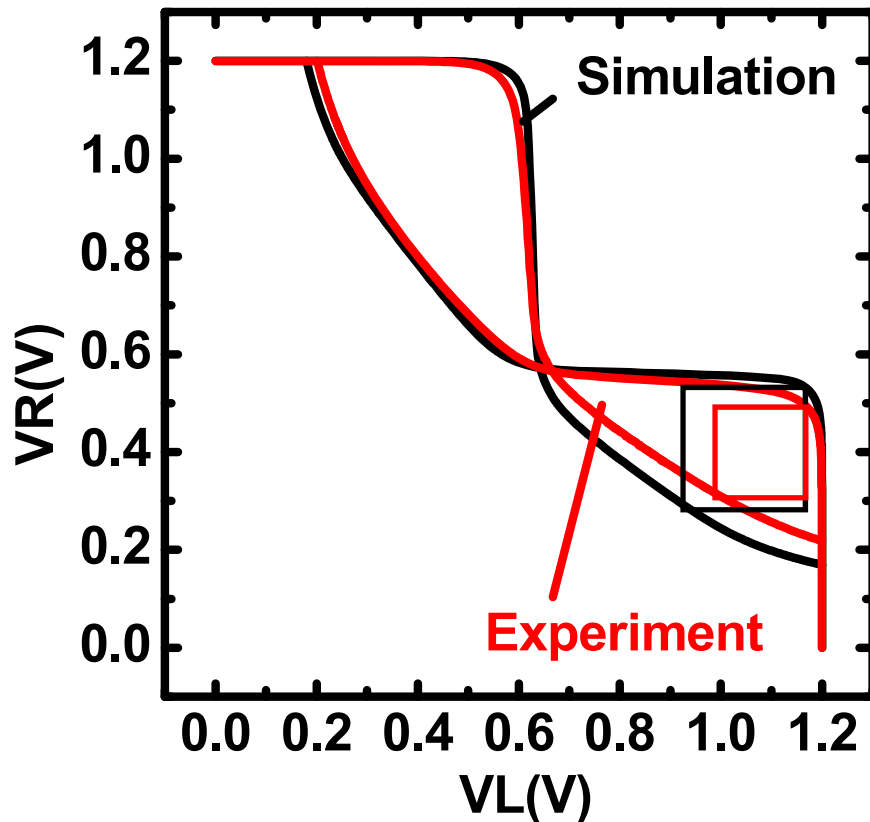
Simulation Using Measured V_{th}



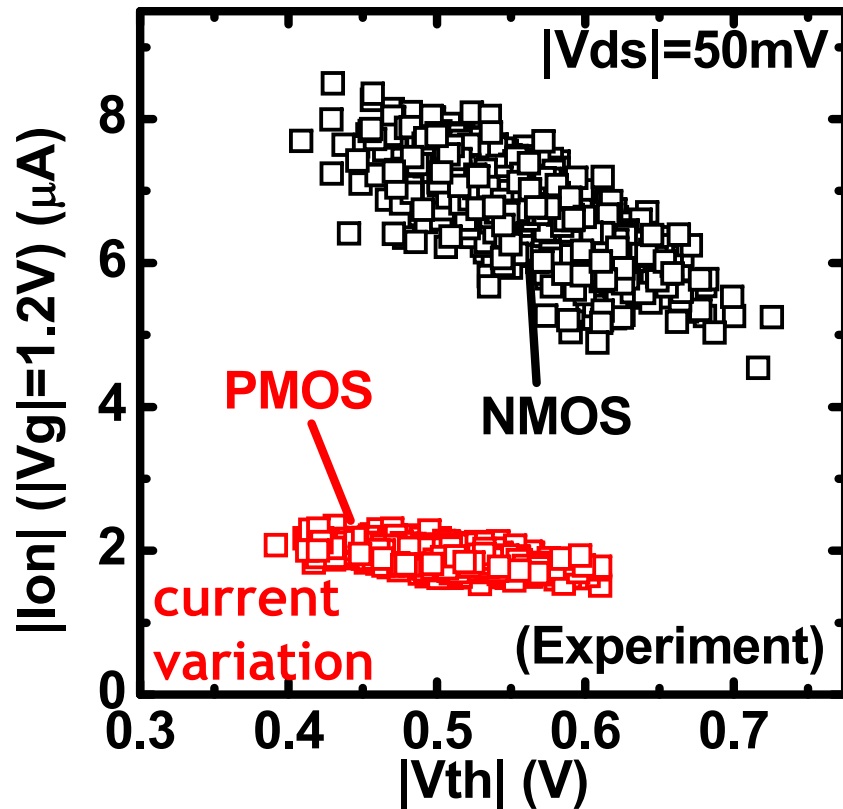
Comparison between Sim and Meas (1k)



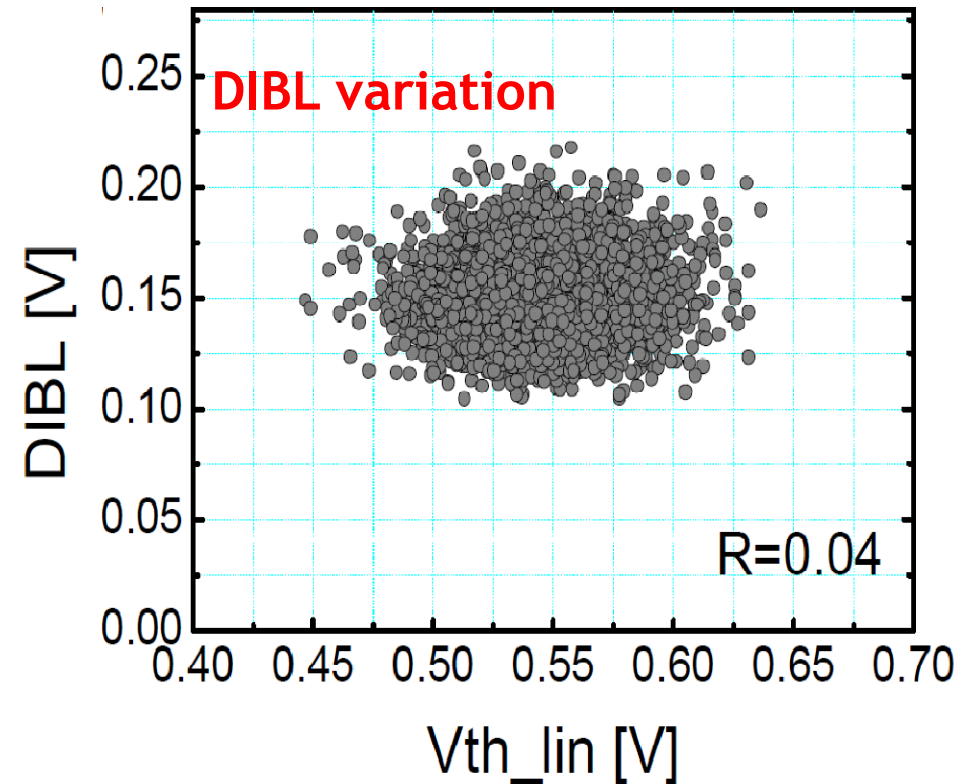
Comparison between Sim and Meas (1k)



Reasons for Disagreement



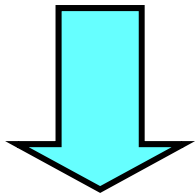
M. Suzuki et al., VLSI Technology Symposium, p. 191, 2010.



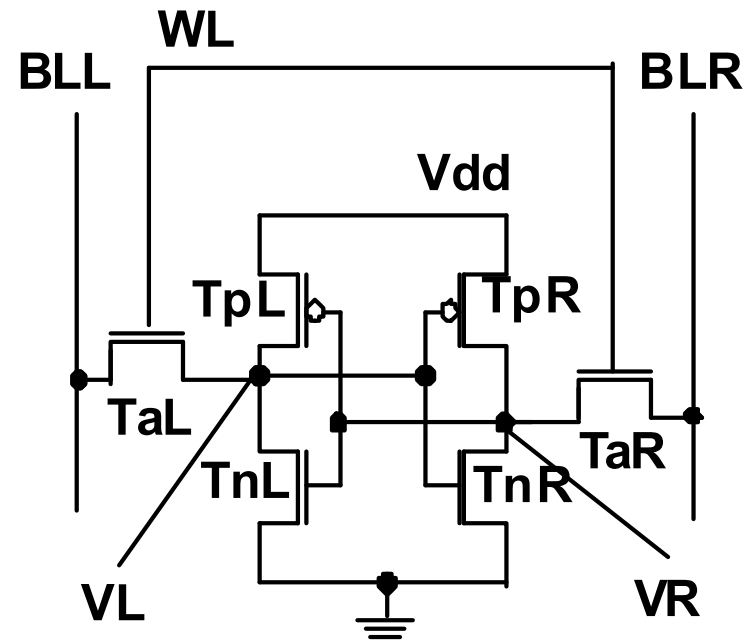
M. Miyamura et al., IEDM, p.447, 2008.

Reasons for Disagreement

- (1) g_m variability?
- (2) DIBL variability?
- (3) Body factor variability?



To be presented in 2010 IEDM



Summary

- 1. Drain current variability is caused by “Current Onset Voltage” Variability, which originates from potential fluctuation by RDF.**
- 2. SNM and V_{th} of individual transistors are directly measured by SRAM DMA TEG. SNM variability is not explained by the V_{th} variability alone.**

This work is performed in the MIRAI-Project supported by NEDO.